

600 Suffolk Street Lowell, MA 01854 Tel (978) 934-4903 Fax (978) 459-7915 http://ulcar.uml.edu

Center for Atmospheric Research College of Arts and Sciences

# **RPI Telemetry Data Model**

A detailed description of the logical and physical data models for telemetry data produced by the RPI instrument on the IMAGE satellite

**Revision 2.8** 

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### **Table of Contents**

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	TABLE OF	Contents	2
	TABLE OF .	ACRONYMS	4
	LIST OF TA	BLES	5
	LIST OF FIG	GURES	6
R	PI TELEN	IETRY DATA MODEL	7
1	GENEF	RAL CONSIDERATIONS	7
	1.1 PU	RPOSE	7
	1.2 Sco	OPE	7
2	RPI OP	PERATING MODES AND DATA PRODUCTS	7
	2.1 AC	TIVE AND PASSIVE OPERATING MODES	7
R	PI SCIEN	CE TELEMETRY DATA MODEL	9
3	RPI SC	IENCE TELEMETRY LOGICAL MODEL	Q
5	21 D.		
	J.I KA	Data volume considerations	۲
	3.1.1 2.1.2	Data loss and commution	9 10
	3.1.2 3.2 DA	Data loss and corruption	10
	3.2 DA	Databin Types	10
	32.1	Fnumerating databins per frequency	10
	323	Ordering databins per frequency	14
	3.3 OP	ERATING MODES. WAVEFORMS AND DATABIN FORMATS	16
1	<b>PPI SC</b>	IENCE TEI EMETRY PHYSICAI MODEI	17
4			···· 17
	4.1 PA	A reference of A ref. A	1 /
	4.1.1	Assignment of ApID to packets	17
	4.1.2	Pucket Structure Design	17
	4.1.5	Filling data section of packet	10 18
	4.1.4	Filling adia section of packet	10 19
	4.2 UE	CCSDS Progmblo	10
	4.2.1	RPI General Header	10
	42.2	Profaco	17
	424	Data Header	17
	4.2.5	Frequency Header	26
	4.2.6	Data Section	26
	4.2.7	Checksum	27
5	CALIB	RATION AND CONVERSION OF MEASURED DATA TO PHYSICAL UNITS	28
	5.1 ON	BOARD DATA PROCESSING	28
	5.1.1	Analog signal processing	28
	5.1.2	Correcting gain and phase differences of X, Y, and Z receiver channels	31
	5.1.3	Default and Dynamic calibration	32
	5.1.4	Phase and Amplitude calibration	33
	5.1.5	Scaling of X and Y channels	33
	5.1.6	Despinning of X and Y channels	33
	5.1.7	Digital signal processing	33
	5.1.8	Linear-to-log signal compression	34

#### UMLCAR RPI Telemetry Data Model v 2.8

5.2	CONVERTING RPI READINGS TO PHYSICAL UNITS	
5.	2.1 Converting range bin number to km	
5.	2.2 Converting amplitude to field strength in $\begin{bmatrix} nVp \\ m \end{bmatrix}$	
5.	2.3 Converting thermal noise amplitudes to [ <sup>dBVrms</sup> / <sub>root-Hz</sub> ]	
5.	2.4 Converting phase data to physical units	
5.	2.5 Converting Doppler bin number to Hz	
5.	2.6 Converting antenna impedance data to physical units	
RPI L	EVEL 0 HOUSE KEEPING DATA FORMATS	41
6 H	OUSE KEEPING DATA	
61	( <b>R</b> HK) HOUSE KEEDING DATA SETS $\Delta pID = 0x02$	41
6.1	(K_IK) HOUSE KEELING DATA SETS. AT ID 0X02	
0. 6	1.1 Housekeeping fielder	
0. 6	1.2 Miscellaneous status information	
0. 6	1.5 Digital Sensor Reduings	
0. 6	1.4 Analog Sensor Readings	
0. 6	1.5 NOGO TADIE	
0.	1.0 KP1 POWER LIMITS	
0.2	(K_SKD) SEGMENT REPORT DATA SET. APID=0x04	
0.	2.1 Segment Data	
0.5	(K_MSO) SUFTWARE MESSAGE. APID=0X00	
0.	5.1  50 jiware Message	
0.4	(R_ECH) COMMAND ECHO. APID=0X08	
0.	4.1 Commana Replica	
<b>RPI D</b>	EVELOPMENT PACKET FORMATS	
		10
7 D	EVELOPMENT PACKET FORMATS	
7.1	APID=0x1F Frequency Set Response Packet	
7.2	APID=0x2F Memory Read/Write Response Packet	49
7.3	APID=0x3F VME READ/WRITE RESPONSE PACKET	
7.4	APID=0x4F Digitizer Samples Packet	
APPE	NDIX A. THERMAL NOISE DATA PROCESSING	
A 1		~ 1
AI.	CALCULATING LOG AMPLITUDES	
A2.	CALCULATING CROSS POWER TERMS (XY, XZ AND YZ)	
A3.	CALCULATING CROSS PHASES (XY, XZ AND YZ)	
APPE	NDIX B. COUPLER BAND CENTER FREQUENCY TABLE	
APPE	NDIX C. CALIBRATION PROCEDURES	54
C1.	PHASE CALIBRATION PROCEDURE	
C2.	ONBOARD CALIBRATION PROCEDURE	
C3.	AMPLITUDE CALIBRATION PROCEDURE	
C.	3.1. Input voltage calculation	
C.	3.2. Amplitude calibration coefficients	
	▲ <i>00</i>	

3

### Table of Acronyms

ApID	:	Application ID (Telemetry Record Type)
BIT	:	Built In Test.
CDF	:	Common Data Format.
CIDP	:	Central Instrument Data Processor
CIT	:	Coherent Integration Time
DBD	:	Double Byte Data
HKD	:	House Keeping Data.
ICD	:	Interface Control Document.
IDFS	:	Instrument Data File Set
LTD	:	Linear Time-domain Data.
LSD	:	Linear Science Data
MET	:	Mission Elapsed Time
PPS	:	Pulses Per Second
PRD	:	Precision Range Data.
RMS	:	Root Mean Square
RPI	:	Radio Plasma Imager
SBD	:	Single Byte Data.
S/C	:	Spacecraft
SI	:	Science Instrument.
SMD	:	Spectral Maximum Data.
SPS	:	Staggered Pulse Sequence.
SSD	:	Standard Science Data.
SST	:	Schedule Start Time.
TN	:	Thermal Noise.
TPC	:	Transmitter Power Card.
TTD	:	Thermal Time-domain Data.

### List of Tables

Table 3.2-1	Number of databins per 1 frequency	. 14
Table 3.3-1	Operating Modes, Waveforms and Databin Formats	. 16
Table 4.1-1	ApID Assignment	. 17
Table 4.2-1	General Structure of RPI Science Data Packet	. 18
Table 4.2-2	CCSDS Preamble, Primary Header	. 19
Table 4.2-3	CCSDS Preamble, Time Tag	. 19
Table 4.2-4	RPI General Header	. 19
Table 4.2-5	Preface	. 20
Table 4.2-6	Data Header	. 22
Table 4.2-7	Frequency Header	. 26
<i>Table 4.2-8</i>	Checksum	. 27
Table 5.1-1	Nominal receiver voltage gains (X, Y, and Z) for various settings of G, in dB relative to the	
minimum gain	at G=1	. 30
<i>Table 5.1-2</i>	Measured receiver voltage gains for various settings of G, in dB relative to the minimum gain	п
at $G=1$ .	30	
Table 5.2-1	Physical units for RPI science data	. 35
Table 5.2-2	Doppler shift frequency	. 40
Table 5.2-3	Antenna impedance data in physical units	. 40
Table 6.1-1	Universal RPI Housekeeping packet format	. 41
Table 6.1-2	HK Header	. 41
Table 6.2-1	RPI House Keeping data format	. 42
Table 6.2-3	Miscellaneous status information	. 42
Table 6.2-4	Digital sensor readings	. 42
Table 6.2-5	Digital Sensor Readings	. 43
<i>Table</i> 6.2-6	Analog sensor readings	. 43
Table 6.2-7	NoGo Table	. 44
<i>Table 6.2-8</i>	Digital and Analog sensor flag parameters	. 44
Table 6.1-9	Peak and Average Power Limits	. 45
Table 6.3-1	RPI Segment Report data format	. 45
Table 6.3-2	Segment Data	. 45
Table 6.4-1	RPI Segment Report data format	. 45
Table 6.4-2	Software message	. 46
Table 6.4-3	Message Codes and Parameters	. 46
Table 6.5-1	RPI Command Echo format	. 47
Table 6.5-2	Command Replica	. 47
Table 7.1-1	Frequency Set Response packet, ApID=0x1F	. 48
Table 7.2-1	Memory Read/Write Response packet, ApID=0x2F	. 49
Table 7.3-1	VME Read/Write Response packet, ApID=0x3F	. 49
Table 7.4-1	Digitizer Sample packet, ApID=0x4F	. 50
Table C3-1	X/Y Amplitude Corrections and Physical Units table.	. 58

## List of Figures

Figure 2.1-1	RPI plasmagram measurement	8
Figure 2.1-2	RPI dynamic spectrogram	8
Figure 3.2-1	Linear Time Domain (LTD) databin	. 10
Figure 3.2-2	Spectral Science Data (SSD) databin	. 11
Figure 3.2-3	Spectral Maximum Data (SMD) databin	. 11
<i>Figure 3.2-4.</i>	Precision Group Data (PRD) databin	. 12
Figure 3.2-5	Calibration Data (CAL) databin	. 12
Figure 3.2-6	Double and Single Byte Data (DBD, SBD) databins	. 13
Figure 3.2-7	Thermal-noise Time-domain Data (TTD) databin	. 13
Figure 4.2-1	Example of nominal frequency calculations: linear steps, 4 multiplexed frequencies	. 23
Figure 5.1-2	Three signal processing channels in RPI.	. 29
Figure 5.1-3	Voltage gain of receivers with preamplifiers for gain $G = 15$	. 31
Figure 5.1-4	Desired effect of amplitude and phase corrections to X and Y output voltages.	. 32
Figure 5.2-5	Conversion of amplitudes to physical units	. 36
Figure 5.2-6	Physical units conversion for thermal noise data	. 39
Figure C1-1	Phase calibration setup with HP synthesizer	. 54
Figure C2-1	Application of calibration signals to X(Y) and Z receiver channels	. 55
Figure C3-1	Amplitude calibration setup with HP synthesizer	. 56
Figure C3-2	Z channel voltage per digitizer unit, [nV]	. 57

## **RPI Telemetry Data Model**

#### **1** General Considerations

#### 1.1 Purpose

The purpose of this document is to describe RPI Telemetry Data Model that is used by the RPI instrument on the IMAGE satellite to produce full resolution science and housekeeping telemetry data. The Data Model consists of

- a <u>logical data model</u> describing all telemetry data elements, their relationship and organization, and
- a <u>physical data model</u> describing data packetization and physical presentation of the data elements in the telemetry packets.

#### 1.2 Scope

The Data Model describes presentation of the following physical quantities:

- Antenna voltage samples acquired by the RPI in its Active Sounding and Passive Reception operational modes, together with their measurement attributes
- Auxiliary housekeeping data that include Built-In Test status, software messages, and memory content dump.

#### 2 RPI Operating Modes and Data Products

#### 2.1 Active and Passive operating modes

The RPI instrument is a low-power active/passive radar which operates in the radio frequency bands that contain the plasma resonance frequencies characteristic of the Earth's magnetophere (3 kHz to 3 MHz). The RPI consists of a 10W radio transmitter that emits radio signals propagating through magnetospheric plasma medium, and a sensitive 3-channel receiver system mated to two 500 m dipole wire antennae and one 20 m lattice boom dipole antenna.

In its active operarting mode, RPI can locate remote regions of various plasma densities by observing radar echoes. For the RPI transmitter signal to reflect from a remote plasma structure, return to the spacecraft location, and remain above the noise level, a number of conditions have to be met. RPI signals are reflected where the radio frequency is equal to the plasma frequency, and direction of the signal propagation is normal to the local plasma isodensity contour. By stepping through various frequencies for the transmitted signal, features of various plasma densities can be observed.

Resulting data product is RPI plasmagram, an image in which received signal strength (color scale) is a function of echo delay (range in vertical scale) and radio-sounder

frequency (horizontal scale) of the radar pulses (Figure 2.1-1). Radar echoes from important magnetospheric structures, such as the magnetopause and the plasmapause, appear as traces on plasmagrams. Plasmagram traces are intermixed with vertical signatures corresponding to the plasma resonances excited locally by the transmitted signal and various natural emissions propagating in space.



Figure 2.1-1 RPI plasmagram measurement

Purpose of the RPI passive radio observation is to detect natural emissions present in the magnetosphere and plasmasphere of the Earth at frequencies between 3 kHz and 3 MHz. Similar to the plasmagram mode, RPI receivers are stepping through various frequencies to observe radio emissions.

Passive-mode observations admit visual presentation as dynamic spectrogram, in which received signal strength (color scale) is a function of frequency (range in vertical scale) and time (horizontal scale) ().



Figure 2.1-2 RPI dynamic spectrogram

## **RPI Science Telemetry Data Model**

#### 3 RPI Science Telemetry Logical Model

#### 3.1 Rationale for Data Model Design

#### 3.1.1 Data volume considerations

RPI is capable of producing data volumes much too high for the telemetry channel throughput. For example, with 5% logarithmic stepping through the nominal frequency band, 128 ranges, 16 repetitions per frequency and 2 polarizations, total data volume collected during a single RPI active sounding measurement is

(12 bit in-phase +12 bit quadrature samples) \*
3 antennas \*
16 Doppler lines \*
128 ranges \*
2 polarizations
\* 142 frequencies = 5,234,688 bytes

With provision of up to 256 Doppler lines, 1024 ranges and smaller frequency steps these volumes may become even larger.

To overcome the problem of high data traffic, a number of measures is devised.

- **Onboard Rice Lossless compression** performed by CIDP.
- **Data thresholding**, which can substantially improve compression ratio.
- **Logarithmic (lossy) compression**. 33% data reduction can be achieved by storing 8 bit logarithmic scale amplitudes and 8 bit phases instead of 12 bit linear scale quadrature components.
- Storing phase differences instead of absolute phases. 16% reduction of spectral data per range bin comes from storing two phase differences relative to the third phase instead of three phases of all three antennas.
- **Collapsing of complete Doppler spectrum to one Doppler line** by selecting the spectrum peak. This is equivalent to considering only one echo per range.
- Collapsing three antennae to one antenna by r.m.s. averaging of amplitudes.

It is not necessary to apply all data reduction measures simultaneously. Only onboard compression of data by CIDP is performed always on all RPI data categories. Data thresholding ratio is specified as a measurement program parameter Z (see *RPI Commanding* document, Section 1.4.2, Table 1.4-1) which can be optimally adjusted by RPI flight software to control data volume. Logarithmic compression proved to be efficient for storage of spectral domain data (see Section 1.1.1 below), and in this case phase differences are always stored instead of absolute phases. Collapsing spectrum and antenna data are strong measures affecting amount of science information and should be used with caution.

#### 3.1.2 Data loss and corruption

Data model design has to consider possibility of partial loss or corruption of individual data sections due to downlink errors and dropouts. Loss of a part of the RPI data record should not cause consequent problems in reading the rest of the data record.

#### 3.2 Databin

Logical Data Model for RPI telemetry data uses concept of enumerated databins. A databin is a basic measurement data element holding antenna voltage samples acquired for a particular frequency and range. The databin concept allows single data representation that is universally applicable to RPI measurements conducted with various combinations of the operating parameters and onboard data reduction schemes. Enumeration of the databins pertaining to the same measurement makes it possible to restore databin attributes even if some of the databins in the original set were damaged or lost.

#### 3.2.1 Databin Types

The databin consists of all measurement data associated with a single frequency/range/Doppler bin (i.e. log amplitude and phase bytes, or alternately real and imaginary amplitudes for 1 or 3 antennas, Doppler shift value). Figure 3.2-1 shows Linear Time Domain (LTD) databin contents. The antenna voltages are sampled twice with 90° phase delay to obtain two 12 bit quadratures per antenna, totaling 9 bytes per databin. The LTD format can be best used for time-domain data (SPS mode, relaxation sounding, chirp sounding).



Figure 3.2-1 Linear Time Domain (LTD) databin

A more compact Spectral Science Data (SSD) databin (see Figure 3.2-2) is best suited for storing individual lines of the Doppler spectrum.



Logarithmic scale 8 bit amplitude 8 bit phase differences 8\*5 = 40 bits = 5 bytes total

Figure 3.2-2 Spectral Science Data (SSD) databin

SSD databin can be obtained from the LTD databin by:

- converting the quadratures to a "polar" representation (i.e., amplitude and phase),
- reducing them to 8 bits (logarithmic compression for the amplitude), and
- subtracting phase of antenna Z from the all phases.

Collapsing of complete Doppler spectrum to one line involves subsequent storage of its Doppler number in the output data bin. Corresponding format 3-Log Polar/8-reduced is shown in Figure 3.2-3.



Figure 3.2-3 Spectral Maximum Data (SMD) databin

Precision Group Range technique involves sounding on two closely spaced frequencies with reduction of both frequency data to one Doppler line and calculating phase differences

with respect to selected phase on the second frequency. The PRD format (Figure 3.2-4) requires storing three amplitudes, five phase differences and one Doppler line.



Figure 3.2-4. Precision Group Data (PRD) databin

Figure 3.2-5 shows the databin contents for calibration data, which is very similar to SMD or SSD formats, but stores three amplitudes and three (absolute) phases.



Figure 3.2-5 Calibration Data (CAL) databin

Another two formats are envisioned to store one antenna data, with r.m.s. average amplitude calculated over three antennas. Double Byte Data (DBD) databin stores 1 byte log scale r.m.s. amplitude and 1 byte Doppler number (Figure 3.2-6). SBD (Single Byte Data) databin further reduces resolution of amplitude and Doppler to fit them in 1 byte.



Figure 3.2-6 Double and Single Byte Data (DBD, SBD) databins

Finally, a databin format is provided for the Thermal noise Time-domain Data (TTD), shown in Figure 3.2-7. In this measurement mode, the following operations are made for each frequency:

	Anten	Anten	Anten		Byte #	Byte Contents
		na	na \		00	A1, antenna X
$\backslash$	* \	~ \	1 /	<b>`</b>	01	A1, antenna Y
8 Averaged Log					02	A1, antenna Z
Amplitudes	A1	A1	AI		03	A2, antenna X
(time domain)					04	A2, antenna Y
· · · · ·	A2	A2	A2		05	A2, antenna Z
	A3	A3	A3			
						•
	A4	A4	A4		21	A8, antenna X
·					22	A8, antenna Y
	A5	A5	A5		23	A8, antenna Z
					24	CP Magnitude XY
	A6	A6	A6		25	CP Magnitude XZ
					26	CP Magnitude YZ
	A7	A7	A7		27	CP Phase XY
-					28	CP Phase XZ
	<b>A</b> 8	48	48		29	CP Phase YZ
	AU	7.0	~~~			
Magnitude of cross-power term	M <sub>XY</sub>	M <sub>xz</sub>	M <sub>YZ</sub>			
Dhann of succe power to an	_	_	_	1	Logarithmic s	cale 8 bit averaged amplitudes
mase of closs-power term	P <sub>XY</sub>	P <sub>xz</sub>	P <sub>YZ</sub>		Logarithmic s	cale 8 bit cross power magnitude
L			1	1	8 DIT CROSS PO	wer pnases
					to bytes per a	antenna, so bytes total

#### Figure 3.2-7 Thermal-noise Time-domain Data (TTD) databin

1. For each antenna,  $4(2^N)+4$  raw quadrature samples are collected. N is the standard RPI parameter used to specify number of transmitted pulses. No transmission is done

in the thermal noise mode, and all samples are taken consecutively with 3.2 ms sampling period.

- 2. 2<sup>N</sup> averaged log amplitudes are computed using 8-point sliding window with 50% overlay.
- 3. For each set of 8 averaged amplitudes (36 raw quadrature samples), three cross-power terms are calculated (corresponding to the antenna pairs XY, XZ, and YZ).

One TTD databin accommodates:

- eight averaged amplitudes per antenna, totaling  $8 \times 3 = 24$  logarithmic scale amplitudes, and
- one set of the amplitude and phase of the cross-power terms XY, XZ, and YZ.

Total size of one TTD databin is therefore 24+6 = 30 bytes. Minimum 36 samples (N=3) per antenna have to be collected to produce a good data packet with a single TTD databin per frequency. Maximum value of N is 8, with 32 TTD databins per frequency.

A detailed description of onboard thermal noise data processing is given in Appendix A.

#### 3.2.2 Enumerating databins per frequency

The data model design suggests enumeration of all <u>databin</u> types (Figure 3.2-1 - Figure 3.2-7) collected at a particular frequency. Table 3.2-1 enlists the expected number of databins for available RPI measurement modes, signal waveforms, and databin formats.

Mode Waveform		Databin format	Number of databins per 1 frequency		
	SPS [X]=3	LTD	# of ranges * # polarizations		
		LTD	# Doppler lines * # of ranges * # polarizations		
		SSD	# Dopplet lines $#$ of ranges $#$ polarizations		
	Pulse modes	SMD			
Sounding	[X]=1,4,5,8,9	DBD	# of ranges * # polarizations		
		SBD			
[0]-3		PRD			
		SSD	# Doppler lines * # of ranges * # polarizations		
	Chirp [X]=2	SMD			
		DBD	# of ranges * # polarizations		
		SBD			
		LTD	<pre># repetitions * # of ranges * # polarizations</pre>		
Relaxation	Short pulse		# of ranges * # polarizations		
[O]=R	[X]=5				
Whistler	0.5 sec pulse		$\pi$ of ranges $\pi$ polarizations		
[O]=W	[X]=6				
Calibration	Short Pulse	CAL	1		
[O]=C	[X]=5	CAL			

Table 3.2-1Number of databins per 1 frequency

#### 3.2.3 Ordering databins per frequency

The order in which the databins are stored is always the same:

- 1. Doppler line #1 to  $2^{N}$  (program parameter N is # of repetitions) (*fastest index*)
- 2. Range #
- 3. Polarization

With this arrangement, any given databin number can be converted to the databin's range bin #, polarization and, if used, Doppler line # or repetition #. The following

equations for databin number apply:

$$\widetilde{N}_{DB} = \widetilde{d} + \widetilde{r} \cdot D + \widetilde{p} \cdot D \cdot R \tag{3.2-1}$$

where

$\widetilde{N}_{DB}$	= databin number
D	= total number of Doppler lines,
R	= total number of ranges (always assumed 1 for TTD databin)
$\widetilde{d}$	= databin Doppler line
ĩ	= databin range bin number
$\widetilde{p}$	= databin polarization
~	

means numbering from 0 to n-1 instead of 1 to n.

Restoring of databin parameters is done as follows:

$$\widetilde{p} = \left\lfloor \frac{\widetilde{N}_{DB}}{D \cdot R} \right\rfloor$$
(3.2-2)

$$\widetilde{n}_{DB} = \widetilde{N}_{DB} \mod \left( D \cdot R \right) \tag{3.2-3}$$

$$\widetilde{r} = \left\lfloor \frac{\widetilde{n}_{DB}}{D} \right\rfloor \tag{3.2-4}$$

$$\widetilde{d} = \widetilde{n}_{DB} \mod D \tag{3.2-5}$$

Let's consider the following example:

RPI Sounding, Complimentary Code X=1, SSD databin, 16 Doppler lines, 64 ranges, 2 polarization. Total number of databins per frequency is 16\*64\*2 = 2048. The databin at Doppler line d = 4 of 16, range r = 8 of 64 and polarization p = 2 of 2 has databin serial number, according to (3.2-1),

$$N_{DB} = \tilde{N}_{DB} + 1 = (4 - 1) + (8 - 1) \cdot 64 + (2 - 1) \cdot (8 \cdot 64) + 1 = 1140 \quad (\text{of } 2048)$$

Reverse calculations using (3.2-2-3.2-5) give:

(slowest index)

$$p = \left\lfloor \frac{1139}{16 \cdot 64} \right\rfloor + 1 = 2 \quad (\text{of } 2)$$
  

$$\widetilde{n}_{DB} = 1139 \mod 1024 = 115$$
  

$$r = \widetilde{r} + 1 = \left\lfloor \frac{115}{16} \right\rfloor + 1 = 8 \text{ (of } 64)$$
  

$$d = \widetilde{d} + 1 = 115 \mod 16 + 1 = 4 \text{ (of } 16)$$

#### 3.3 Operating Modes, Waveforms and Databin Formats

Table 3.3-1 reviews the available choice of RPI scientific data formats, depending on selection of operating mode and waveform.

Operating Mode	Waveform	Databin Type	L0.5 Data Format	L1 Data Format	
	SPS	LTD			
	Chirp	DBD			
Active Sounding	Complimentary code	LTD	UDE	CDF	
[O]=S	Long pulse	SMD	UDF	Plasmagram	
	Short pulse	PRD SSD			
Passive Reception [O]=T	none	TTD	UDF	CDF Dynamic Spectrogram	
Relaxation [O]=R	Short pulse	LTD	UDF	CDF Plasmagram	
Whistler	0.5 sec pulse	LTD	UDF	CDF Plasmagram	
[O]=w	1.95 sec pulse	No output	N/A	N/A	
Calibration [O]=C	Short pulse	CAL	UDF	N/A	

Table 3.3-1 Operating Modes, Waveforms and Databin Formats

#### 4 RPI Science Telemetry Physical Model

#### 4.1 Partitioning data in instrument packets

Enumerated databins are partitioned in instrument packets for delivery to the ground station.

#### 4.1.1 Assignment of ApID to packets

The instrument packets are assigned an ApID value to group data of similar content in packets of the same ApID. The ApID allocation is done by the databin format as indicated in Table 4.1-1.

Databin	CAL	DBD	LTD	SMD	SBD	PRD	SSD	TTD
Preface [D]	1	2	3	4	5	6	7	8
ApID	0x0C	0x20	0x30	0x40	0x50	0x60	0x70	0x10

Table 4.1-1 ApID Assignment

In addition to 8 ApIDs assigned to the science packets, there are four types of the data packets used during development only. The "development" packets are listed and described in Section 8.

#### 4.1.2 Packet Structure Design

Arrangement of data into packets imposes two constrains on the data format design:

- 1. Packets of the same ApID must have a fixed size.
- 2. Design should be robust to the loss of some packets during transfer.

A provision must be made to store, for each frequency, the following auxiliary information:

- 1. MET offset from nadir to calculate spin phase
- 2. Frequency offset obtained during search of the quietest frequency
- 3. Autogain selection
- 4. Antenna Impedance data

The size of data collected at a single frequency may vary substantially. In relaxation sounding mode with 8 ranges, 1 polarization, and single byte SBD content total amount of data per frequency is 8 bytes. In a regular sounding with N=5 (32 Doppler lines), 128 ranges, 2 polarizations and 5 byte SSD content the data per frequency amounts to 40,960 bytes. Thus, structuring of data into packets has to account for possible irregular insertion of auxiliary frequency information in the data.

#### 4.1.3 Headers with auxiliary information

There are two types of headers designed to store complete per-frequency auxiliary information and ensure proper data handling in case of telemetry loss. A **Data Header** is stored once per packet with Frequency reading, MET nadir offset time and databin serial number related to the first databin in the data portion of the packet. The Data Header provides information necessary to proceed with data unpacking in case of missing previous telemetry packet. A **Frequency Header** precedes each numerated sequence of databins, containing autogain and frequency search settings, most probable amplitude, and antenna impedance characteristics. The Frequency Header provides necessary per-frequency information.

Detailed description of the headers can be found in Section 4.2.5.

#### 4.1.4 Filling data section of packet

There is no difference in arrangement of the packet for different science data other than contents of the databins. The databins are stored in a packet one by one in accordance to the order described in section 3.2.3 (Next Doppler line# - next range – next polarization). The length of data section in packets is fixed at 3072 bytes (to meet the requirement to have fixed packet lengths for particular ApID). When the end of the defined 3072 byte data section is reached and no more databins can fit the packet, the unused part is zero filled. But, if the end of one frequency is reached before the end of the data block is reached, a frequency header is inserted (again, if there is no room for the frequency header at the end of the data block the block is zero filled). Each new data block contains enough information in the header to identify the first data bin contents, even if the preceding telemetry block is lost.

#### 4.2 General Structure of RPI Data Packet

All Scientific Data Formats have identical general structure of the packet as indicated in Table 4.2-1. The structure always includes CCSDS Preamble, General Header, Preface, Data Header, Frequency Header, Data Section, and Checksum.

Sec_2.1	Sec_2.2	Sec_2.3	Sec_2.4	Sec_2.5	Sec_2.6	Sec_2.7
CCSDS	General	Preface	Data Header	Frequency	Data Section	Checksum
Preamble	Header			Header		
(12 bytes)	(3 bytes)	(103 bytes)	(13 bytes)	(10 bytes)	(3072 bytes)	(1 byte)

Table 4.2-1 General Structure of RPI Science Data Packet

#### 4.2.1 CCSDS Preamble

The standard CCSDS preamble consists of 6 byte Primary Header and 6 byte Time Tag, as shown in Table 4.2-2 and Table 4.2-3.

Byte Count No.	Byte Offset No.	Byte Length	Description	Units	Туре	Range
01	01	2	16 bit ApID data: HHHHHiiiiAAAAAAA H- header indicator i – instrument ID A – ApID	N/A	Hex	N/A
23	23	2	Sequence Counter	N/A	Unsigned short	N/A
45	45	2	Byte Count	N/A	Unsigned short	0-65535

 Table 4.2-2
 CCSDS Preamble, Primary Header

#### Table 4.2-3 CCSDS Preamble, Time Tag

Byte Count No.	Byte Offset No.	Byte Length	Description	Units	Туре	Range
69	69	4	MET Coarse Time	100 ms	Unsigned long	0 to 4294967296
1011	1011	2	MET Fine Time	195.3125 us	Short	0, 128-65408

#### 4.2.2 RPI General Header

The general header format is standard for all science data packets. The only difference is in the value content of the ApID. The header identifies the data type, the preface length and the software version number.

Table 4.2-4 RPI General Header

Byte Count No.	Byte Offset No.	Byte Length	Description	Units	Туре	Range
12	0	1	Application Identification ApID	N/A	int	exact
13	1	1	Preface length	N/A	int	100
14	2	1	Software Version Number	N/A	int	0-255

#### 4.2.3 Preface

The "Preface" is standard to for all science data. The Preface (Table 4.2-5) contains the data headers that serve to tag the time/satellite characteristics for each measurement as well as list the required parameters to identify the RPI mode of operation. Unless otherwise specified all values are integers. Note: items in the "description" column that are followed by a bracketed abbreviation (e.g. [L]) correspond exactly to measurement parameters specified in the program parameters in the "Measurement Parameter Table" data (see *RPI Commanding* document, Section 1.4, Table 1.4-1).

Byte	Byte	Byte	Code				
Count	Offset	Len		Description	Units	Туре	Range
<b>NO.</b>	No.	4		Mission Elenged Time of last nodir [MET]	100	Long	0 to
1318	05	4		Stamp	millisee	Long	010
19	Δ	1		Schedule #	N/A	Byte	4294907290
20	+ 5	1		Program #	N/A	Byte	1-52
20	67	2	01(T)	$\Gamma$ lower Frequency Limit	1kHz	Short	3kHz-3MHz
2122 23.24	8.9	2	01(L)	Coarse Frequency	IKIIZ	Short	JKHZ-JWHZ
2324	0	2	02(0)	If $> 0 \log$ steps	1%	Short	1-100%
				If $< 0$ linear steps	100 Hz		100Hz-
					100112		1MHz
2526	1011	2	03 (U)	Upper Frequency Limit	1kHz	Short	3kHz-3MHz
2728	1213	2	04 (F)	Fine Frequency Step	100 Hz	Short	100Hz-
				1 5 1			1MHz
29	14.	1	05 (S)	No. of fine steps	Unit	Byte	+1 to +8
				(no zero value)			-1 to -8
				negative value disables multiplexing			
3033	1518	4	06 (X)	Tx Waveform *	Table	Four	-9 to +9
				0 = no waveform (passive msmt)		signed	(no zero
				1 = Complimentary (51 msec)		bytes	value)
				2 = FM/CW "Chirp" (125 msec)			Each byte
				3 = Staggered Pulse (786 chips)			contains
				4 = Long Pulse (125 msec)			information
				5 = Short Pulse (3.2 msec)			on a
				6 = 0.5  sec Pulse			waveform
				7 = 1.95 sec Pulse			used in the
				8 = 8 chip complimentary pulse (25 msec)			run
				9 = 4 chip complimentary pulse (13 msec)			
				-1 to –9 same but no phase switching			
				up to four multiplexea waveforms are			
24 27	10.22	4	$07(\Lambda)$	Supported	Tabla	Four	$9 \text{ to } \pm 9$
5457	1922	4	07(A)	1 - Padio Silent (no Tx)	Table	roui	$-010 \pm 0$
				1 - Kaulo Shent (no 1x) 2 = Y antenna only		bytes	(IIO ZEIO
				3 = V antenna only		bytes	value)
				4 = X + Y in linear polarization			
				5 = Right Circular Polarization RCP			
				6 = Left Circular Polarization LCP			
				7 = RCP & LCP alternate w.r.t. +Z			
				8 = X+Y switch linear Pol by 90°			
				-1 to $-7$ same but bypass antenna coupler			
3841	2326	4	08 (N)	No. of Integrated Repetitions *	2 <sup>N</sup>	Four	-8 to +8
				Negative means power integration instead		signed	
				of coherent integration		bytes	

Table 4.2-5 Preface

#### UMLCAR RPI Telemetry Data Model v 2.8

4245	2730	4	09 (R)	Pulse Repetition Rate*	Table	Four	0, 1, 2, 4,
			. ,	0 = 0.5  pps		bytes	10, 20, 50
				1 = 1.0  pps		5	
				2 = 2.0  pps			
				3 = 4.0  pps			
				10 = 10  pps			
				20 = 20  pps			
				50 = 50  pps			
46-49	31-34	4	10 (O)	Operating Mode*	Table	Four	0 to 5
				0 = Standby		bytes	
				1 = Calibration			
				2 = Relaxation			
				3 = Sounding			
				4 = Thermal Noise			
				5 = Whistler			
				6 = Test Pattern		_	
50	35	1	11 (W)	Power Limit constraint	Watts	Byte	0-120
51	36	1	12 (E)	Start Range 960 km units	1 Mm	Byte	0 to 255
52	37	1	13 (H)	Range Resolution	10 km	Byte	24 or 48
5354	3839	2	14 (M)	No. of range bins	Unit	Byte	8 to 1024
				8, 16, 32, 64, 128, 256, 512, 1024			
55	40	1	15 (G)	Base Gain	Table	Byte	-18 to $+18$
				negative = Fixed Gain			
				positive = Automatic Gain		_	
56	41	1	16 (I)	Frequency Search	Table	Byte	-9 to +9
				0 = Disabled			
				n = 5 freq spaced by $n*244$ Hz			
				negative = Default calibration			
57.50	10 10	2	17 (D)	positive = Dynamic calibration	TT .		1 . 1024
5758	4243	2	17 (P)	No. of ranges stored	Unit	Short	1 to 1024
50	11	1	19 (D)	1-1024 Pottom of rongo window	1 Mm	Duto	0 to $250$ Mm
<u> </u>	44	1	10(D) 10(T)	Top of range window	1 Mm	Byte	0 to 250Mm
61 64	43	1	19(1) 20(D)	Datahin Format*	T MIII Table	Eour	0 to 8
0104	4049	4	20 (D)	$0 = N_0 Data$	Table	roui bytes	0108
				1 = Calibration = CAL		Uytes	
				1 = Calibration = CAL 2 = Double Byte Data = DBD			
				3 = L inear Time Domain $-L$ TD			
				4 = Spectral Maximum Data $-$ SMD			
				5 = Single Byte Data - SBD			
				6 = Precision Range Data – PRD			
				7 = Spectral Science Data – SSD			
				8 = Thermal Time Domain – TTD			
6568	5053	4	21 (Z)	Threshold cleaning, in % *	%	Four	0 to 99
				0 = no thresholding		bytes	
69-71	54-56	3	22	Spare program parameter		Ť	
72	57	1		High RF Noise setting, $0 = n_0$ ,	Unit	Byte	0 or 1
				1 = yes.			
7374	5859	2		CIT length	10 ms	Byte	0 to 650sec
75	60	1		Number of multiplexed programs	unit	Byte	1
7677	6162	2		Data Status Flags	N/A	Short	N/A
7881	6366	4		Spin Axis Inertial X component	2s Co.	Int	-1 to +1
8285	6770	4		Spin Axis Inertial Y component	2s Co.	Int	-1 to +1
8689	7174	4		Spin Axis Inertial Z component	2s Co.	Int	-1 to +1

9093	7578	4	Spin Phase Angle	Deg.	Int	-180 to 180
9497	7982	4	Filtered Spin Rate Magnitude	R/Min	Int	+/- 21.4748
98	8386	4	MET Coarse @ which Star Tracker is	100 ms	Int	0 to
101			valid			4294967296
102.	8790	4	MET coarse time of periapse passage	100 ms	Int	0 to
105						4294967296
106	9192	2	Semi-major axis	1 km	Short	0-65535
107						
108	9394	2	Eccentricity, nominally .4	LSB=	Short	0-1
109				3*10 <sup>-5</sup>		
110	9596	2	Cosine of angle of inclination	LSB=	Short	0-1
111				3*10 <sup>-5</sup>		
112	9798	2	Argument of Perigee	LSB=	Short	0-360
113				$5.5*10^{-3}$		
114	99	2	Longitude of the Ascending Node	LSB=	Short	0-360
115	100			$5.5*10^{-3}$		
116	101	2	Distance to earth center	1 km	Short	0-65535
117	102					

\* indicates up to four parameters may be packed into four bytes. The packing order is *reversed*, i.e., as byte count increases, the program index decreases from 3 to 0.

#### 4.2.4 Data Header

The "Data Header" (see Table 4.2-6) contains information necessary to retrieve the databins correctly in case of telemetry losses. See Section 4.1.3 for detailed description of auxiliary headers.

Byte	Byte	Byte	Description	Units	Туре	Range
Count	Offset	Length				
No.	No.					
118119	01	2	Frequency step number	unit	Short	1-65535
120121	23	2	Time offset from nadir MET	0.1sec	Short	0 to 6553 sec
122-125	47	4	Serial number of the first databin in the	unit	Long	0-262143
			packet, $\widetilde{N}_{DB}$			
126-129	811	4	Total number of databins per frequency	unit	Long	8-262144
130	12	1	Multiplexed program number	unit	Bvte	0-3

Table 4.2-6 Data Header

#### 4.2.4.1 Calculation of nominal frequencies

RPI selects the actual frequency for transmission by searching for the quietest frequency around the nominal frequency. To obtain the actual sounding frequency,

- the nominal frequency shall be calculated using the Frequency Step Number stored in the Data Header,
- the frequency search adjustment shall be applied using Frequency Search parameter from the Frequency Header.

The Frequency Step Number is converted to the corresponding nominal frequency in kHz using information stored in the Preface. For <u>linear frequency stepping</u>, the nominal frequency is:

$$f_{nom} = [L] + \left(-[C]\right) \cdot \left\lfloor \frac{\widetilde{N}}{[S]_a} \right\rfloor + [F] \cdot \left(\widetilde{N} \mod[S]_a\right), \tag{4.2-1}$$

where

[L] is Lower Frequency Limit from the Preface,

[C] is Coarse Frequency Step (reported negative in this case),

[S]<sub>a</sub> is the *absolute value* of Number of Fine Steps,

[F] is Fine Frequency Step, and

 $\widetilde{N}$  is frequency step number from the Data Header.

[...] is the *floor* function (the largest integer smaller than the argument)

mod is modulo function (the remainder of integer division).

Example (see Figure 4.2-1):

$$[L] = 100, [C] = -2000 \text{ (i.e., } 200 \text{ kHz}\text{)}, [S] = -4, [F] = 250 \text{ (i.e., } 25 \text{ kHz}\text{)}, \widetilde{N} = 15$$
$$f_{nom} = 100 + (200) \left| \frac{15}{4} \right| + 25 \cdot (15 \text{ mod } 4) = 100 + 600 + 25 \cdot 3 = 775.0 \text{ kHz}$$



Figure 4.2-1 Example of nominal frequency calculations: linear steps, 4 multiplexed frequencies

For logarithmic frequency stepping, the nominal frequency is:

$$f_{nom} = [L] \left( 1 + \frac{[C]}{100} \right)^{\left\lfloor \frac{\widetilde{N}}{[S]_a} \right\rfloor} + [F] \cdot \left( \widetilde{N} \mod[S]_a \right), \tag{4.2-2}$$

where

[L] is Lower Frequency Limit,[C] is Coarse Frequency Step (in %),

 $[S]_a$  is the absolute value of Number of Fine Steps,

[F] is Fine Frequency Step, and

 $\widetilde{N}$  is frequency step number from the Data Header.

The [S] Fine Steps are linearly spaced.

Example 1:

$$[L]=100, [C]=10, [S]=8, [F]=3, \widetilde{N}=23$$

$$f_{nom} = 100 \cdot \left(1 + \frac{10}{100}\right)^{\left\lfloor \frac{23}{8} \right\rfloor} + 3 \cdot \left(23 \mod 8\right) = 100 \cdot 1.1^2 + 3 \cdot 7 = 121 + 21 = 142.0 \ kHz$$

Example 2:

[L]=3, [C]=5, [S]=1, [F]=don't care, 
$$\tilde{N} = 100$$
  
$$f_{nom} = 3 \cdot \left(1 + \frac{5}{100}\right)^{\left\lfloor \frac{100}{1} \right\rfloor} + X \cdot (100 \text{ mod } 1) = 3 \cdot 1.05^{100} + 0 = 394.5 \text{ kHz}$$

Note that is [C] is a multiple of 3 (3, 6, 9, 12...), the frequency stepping is not "logarithmic", but "coupler band centers" (see explanations below).

For <u>coupler band centers frequency stepping</u>, i.e., when [C] is a positive multiple of 3 (3, 6, 9, 12...) the nominal frequency is taken from a pre-defined table of frequencies. Each of the table frequencies is the center of a coupler band where the maximum efficiency of the tuned transmission is reached. Table of the coupler central frequencies is given in Appendix B.

To convert the frequency index to nominal frequency for the coupler band centers stepping mode, the following procedure shall be used:

- 1. Find the table frequency closest to the Lower Frequency Limit, [*L*]. (The closest table frequency may appear to be lower or higher than [*L*].) The found frequency,  $f_{t0}$ , will be the first sounding frequency in the measurement, and its index,  $\tilde{N}$ , is therefore 0. The index of  $f_{t0}$  in the frequency table will be  $i_{t0}$ .
- 2. Frequency stepping is then done by incrementing the table index,  $i_t$ , from  $i_{t0}$  until the Upper Frequency Limit, [U], is exceeded. The increment to  $i_t$  can be greater than 1 if

faster frequency scanning is required. For [C] equal to 3, 6, 9... the increment to the table index is 1, 2, 3..., correspondingly.

Example 1:

$$[L]=100, [C]=6, [S]=1, [F]=don't care, \tilde{N}=2$$

Closest table frequency to 100 kHz is 100.500 kHz, index #65. As [C] equal to 6, the table will be scanned with index increment of 2, i.e., #65 (100.5 kHz), #67 (105.0 kHz), #69 (111.5 kHz), etc. The frequency with  $\tilde{N} = 2$  is therefore 111.5 kHz.

For <u>fixed frequency measurements</u> (i.e., when [L] is equal to [U]), the nominal frequency is:

$$f_{nom} = [L] + [F] \cdot \left( \widetilde{N} \mod[S]_a \right), \tag{4.2-3}$$

where

[L] is Lower Frequency Limit,

 $[S]_a$  is the absolute value of Number of Fine Steps,

[F] is Fine Frequency Step, and

 $\widetilde{N}$  is frequency step number from the Data Header.

i.e., if no frequency multiplexing is requested (i.e., [S] is 1), all frequencies are equal to [L].

#### 4.2.4.2 Calculation of total number of frequencies

The total number of frequencies sampled in a single RPI measurement run can be obtained using the following calculations.

For linear frequency stepping, the total number of frequencies is:

$$N_{total} = \left(\frac{[U] - [L]}{-[C]} + 1\right) \cdot [S]_a$$
(4.2-4)

where

[L] is Lower Frequency Limit,

[U] is Upper Frequency Limit,

[C] is Coarse Frequency Step, and

[*S*]<sub>a</sub> is the absolute value of Number of Fine Steps.

For logarithmic frequency stepping, the total number of frequencies is:

$$N_{total} = \left[ \frac{\log\left(\frac{U}{L}\right)}{\log\left(1 + \frac{[C]}{100}\right)} + 1.999 \right] \cdot [S]_a$$
(4.2-5)

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For coupler band centers frequency stepping, the total number of frequencies is

$$N_{total} = N_{table} \cdot [S]_a \tag{4.2-6}$$

where  $N_{\text{table}}$  is number of the coarse frequency steps, which in this case have to be calculated using Table B-1 (Appendix B) containing coupler band center frequencies:

$$N_{table} = \frac{(i_{upper} - i_{lower})}{[C]/3} + 1$$
(4.2-7)

where

[C] is Coarse Frequency Step,

 $i_{upper}$  and  $i_{lower}$  are indeces of the Upper Frequency Limit, [U] and Lower Frequency Limit, [L], correspondingly, in the coupler frequency table, found by searching the table frequency closest to the nominal frequency.

For <u>fixed frequency measurements</u>, the total number of different frequencies is  $[S]_a$ , and transmission is repeated [C] times, hence

$$N_{total} = [C] \cdot [S]_a \tag{4.2-8}$$

#### 4.2.5 Frequency Header

The format of Frequency Header is shown in Table 4.2-7.

Byte	Byte	Byte	Description	Units	Туре	Range
Count No.	Offset No.	Length				
131	0	1	Gain offset from base gain (4 MSB) Frequency Search (4 LSB)	double steps n*244Hz	Nibble Nibble	0-3 (0,2,4,6 gain steps) 0 to 4
132	1	1	Most probable amplitude	TBD	Byte	TBD
133	2	1	Current on X antenna [Ix]	10mamp	Byte	0-2.55 amp
134	3	1	Voltage on +X dipole antenna $[V_{x1}]$	10 volt	Byte	0-2550 Volt
135	4	1	Voltage on -X dipole antenna $[V_{x2}]$	10 volt	Byte	0-2550 Volt
136	5	1	Current on Y antenna [Iy]	10mamp	Byte	0-2.55 amp
137	6	1	Voltage on +Y dipole antenna [V <sub>y1</sub> ]	10 volt	Byte	0-2550 Volt
138	7	1	Voltage on -Y dipole antenna $[V_{y2}]$	10 volt	Byte	0-2550 Volt
139-140	8-9	2	First Range Bin	Units	Short	0-511

Table 4.2-7Frequency Header

Storing Frequency Header in each data packet is excessive if more that one packet is required to hold one frequency data, but this measure provides necessary robustness of data format to possible telemetry data losses.

#### 4.2.6 Data Section

Data Section contains an array of databins arranged in the sequential order, possibly with frequency headers. The length of the Data Section is fixed at 3072 bytes.

The Data section can hold more than one frequency data and therefore store Frequency Headers (see Section 4.2.5 for format description) which separate individual frequency data. One Frequency Header is placed in front of every databin sequence, unless the Data Section begins with the first databin of the frequency and therefore the Frequency Header preceding the Data Section (see Section 4.2.5) can be used.

The actual frequency setting is not stored in the Frequency Header. To calculate actual frequency of *n*th frequency data in the packet, the *frequency step number* has to be obtained first by adding the frequency step number from the Data Header (see Section 4.2.4) to *n*. Then, formulas (4.2-1) or (4.2-2) shall be used to obtain the nominal frequency. Finally, the actual frequency is obtained by applying frequency search correction to the nominal frequency:

$$f_{act}(n) = f_{nom}(n) + (FS - 2) \cdot [I] \cdot 244 \ Hz \tag{4.2-9}$$

where FS is frequency search adjustment value from the Frequency Header, and [I] is Frequency Search parameter from the Preface.

#### 4.2.7 Checksum

This section contains 1 byte checksum calculated from byte 7 to end of packet by successively applying Exclusive-Or operation on the bytes of the packet.

<i>Table 4.2-8</i>	Checksum
--------------------	----------

Byte Count No.	Byte Offset No.	Byte Length	Description	Units	Туре	Range
N-1	0	1	Checksum	N/A	Byte	0-255

#### 5 Calibration and conversion of measured data to physical units

#### 5.1 Onboard data processing

Figure 5.1-1 shows a complete diagram of RPI onboard data processing, further detailed in subsequent sections of Chapter 3. For illustration purpose, the diagram indicates an assumed signal of 100 nVp/m in the x, y, and z directions undergoing SSD processing with a gain [G] = 15 and operation at a frequency of 65 kHz. To simplify the example, the phase differences of the receivers are not reflected in the processing. The signal phase is assumed 0° so that the in-phase component *I* is equal to the signal amplitude, and the quadrature component *Q* is zero.



Figure 5.1-1 RPI onboard data processing.

#### 5.1.1 Analog signal processing

Figure 5.1-2 shows the diagram of analog signal processing circuitry of RPI.



Figure 5.1-2 Three signal processing channels in RPI.

As Figure 5.1-2 indicates, there are two equal channels, X and Y, each connected to a 500 m dipole antenna. Channel Z is provided with a shorter, 20 m antenna, and therefore has to compensate for the smaller input signal<sup>1</sup> by yielding a higher voltage gain. The broadband preamplifiers in the Z channel have 4 dB more gain than the X/Y preamplifiers, and the Z receiver has ~10 dB more gain. This results in a ~14 dB higher gain in Z channel, unless the high gain setting is selected in the Z preamp. In the latter case, the Z channel has ~26 dB more gain.

All receivers have selectable gain that can be set fixed or chosen optimally in the autogain mode. X and Y gain setting are always set identical, the Z gain is typically greater because of the shorter Z antenna. There are 18 different combinations of two gains (Z and X/Y) that are encoded in a single value of the nominal gain, [G], as shown in Table 5.1-1. The actual gain readings (in dB above the minimum receiver gain) are provided in Table

<sup>&</sup>lt;sup>1</sup> For frequencies below 300 kHz, the difference in the signal voltages induced in the X/Y antennas are  $\sim 20 \log(500/20) =$ **28** dB higher than in the Z antenna.

5.1-2 for the X, Y, and Z channels. The minimum receiver gain is frequency dependent for all receiver channels, and can be derived from the calibration results as discussed below.

Table 5.1-1 Nominal receiver voltage gains (X, Y, and Z) for various settings of G, in dB relativeto the minimum gain at G=1.

G	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
dB steps	0	+6	+12	+18	+24	+30	+24	+30	+36	+42	+48	+54	+24	+30	+36	+42	+48	+54
Z preamp	low	low	low	low	low	low	hi	hi	hi	hi	hi	hi	low	low	low	low	low	low

Table 5.1-2 Measured receiver voltage gains for various settings of G, in dB relative to the minimum gain at G=1.

G	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
X	0	4.6	10.9	18	24.3	30.7	24.3	30.7	37.1	42.7	49.1	55.5	24.3	30.7	37.1	42.7	49.1	55.5
Y	0	3.8	10.9	20.6	24.4	32.1	24.4	32.1	37.1	47.3	55.	60.	24.4	32.1	37.1	47.3	55.	60.
Z	0	5.2	9.3	20.3	23.5	29.2	35.5	40.6	46.7	56.8	61.9	68.	23.5	28.6	34.7	44.8	49.9	56.

Figure 5.1-3 shows the actual voltage gains in dB of the X, Y, and Z receivers for the gain setting of 15

$$g(f) = 20\log_{10} \frac{V_{out}(f)}{V_{in}(f)}$$
(5.1-1)

where  $V_{out}(f)$  is receiver output voltage before the digitizer, and  $V_{in}(f)$  is input voltage at the antenna terminals. Using the actual gains for G=15 and the table of measured gains relative to the minimum gain (Table 3.1-2), it is possible to calculate the gains for all frequencies and base gain settings.

X-Y-Z Receiver Gains



Figure 5.1-3 Voltage gain of receivers with preamplifiers for gain G = 15.

#### 5.1.2 Correcting gain and phase differences of X, Y, and Z receiver channels

RPI measures the 3 orthogonal components of electric field vectors and derives angleof-arrival of the echoes reflected from magnetospheric plasma. The signals from each antenna go through individual receiver channels that introduce frequency-dependent amplification and phase shifts. Differences between the channel characteristics would introduce errors to angle-of-arrival calculations, unless corrected. Therefore, calibration of the phase and gain characteristics of the receiver channels assumes vital importance to the angle-of-arrival data validity.

To ensure proper compensation of differences between the receiving channels, RPI introduces phase and amplitude corrections, for each sounding frequency, to the quadrature components measured by the X and Y receivers. Channel Z acts as the amplitude and phase reference and therefore is passed through unchanged. The purpose of introducing the corrections is to obtain identical response of all channels to the input signal. Figure 5.1-4 illustrates the correction process, assuming identical field strengths along the x, y, and z directions.

The correction applied to the X and Y channels makes the outputs identical. The actual correction factors are calculated based on measurements of the voltage gain and phase shifts of the receiver channels.



Figure 5.1-4 Desired effect of amplitude and phase corrections to X and Y output voltages.

#### 5.1.3 Default and Dynamic calibration

Two calibration modes are implemented

- 1. "DEFAULT". A *CAL Table* is stored in the flight software with results of the X, Y, Z channel calibrations obtained in the laboratory (see description of the phase calibration procedure in Appendix C). The key disadvantage of the "default" correction algorithm is its inability to reflect the actual variability of the RPI hardware characteristics with temperature, time, mechanical impacts, etc. during the mission. Also, the CAL Table contains data collected for a particular, predefined set of frequencies, and therefore when the actual sounding frequency does not match any of the frequencies in the default CAL Table, the algorithm has to select the closest available frequency instead.
- 2. "DYNAMIC": RPI has calibration circuitry that allows the attenuated transmitter signal to go through the receiver channels. The measured receiver response can be directly used to compensate for the inequalities. The dynamic calibration senses the actual receiver characteristics for each sounding frequency immediately before the transmission starts. However, the calibration signals for the X/Y channels are affected by the impedance characteristics of the antennas and therefore the calibration voltages applied at the receiver inputs vary with frequency. A loopback laboratory calibration was conducted to measure the amplitude and phase of the calibration source signal. Further description of the loopback calibration is given in Appendix C.

Either "default" or "dynamic" calibration can be selected in the RPI measurement programs. When dynamic calibration is chosen, it must be combined with the frequency search procedure as both of them are performed during the period of time allocated for the frequency search. Calibration data, regardless of their origin, are reported into the telemetry channel in a data packet with ApID = 0x0C. The unified data format (see Section 2) is used to hold calibration data; <u>however</u>, there are no frequency headers in the Data Section of the <u>CAL packets (see section 2.6)</u>.

#### 5.1.4 Phase and Amplitude calibration

Gain and phase characteristics of the analog circuitry were studied in laboratory conditions, as described in detail in Appendix C.

#### 5.1.5 Scaling of X and Y channels

For low Z preamp gain, the Z axis channel has  $\sim 14$  dB more gain than X and Y, but the output signals from the X and Y channels will typically be larger due to the different antenna lengths. An appropriate scaling is required to optimally packet all data for telemetry and avoid data storage related saturation of the X and Y readings. The scaling factor of 1/8 is introduced for the X and Y channel data, which has to be removed during ground data processing to return to the case of matched X, Y, Z channels.

#### 5.1.6 Despinning of X and Y channels

After the differences in X and Y channels are removed by calibration, it becomes possible to compensate for the spinning of the X and Y antennas (nominally at 1/2 rpm). The despinning procedure calculates the projection of the E-field vector in the x', y', z' system, where

- the *x*' axis points to the center of the Earth,
- the z' axis, equal to the z axis, points in the direction of the orbital angular momentum, and
- the y' axis is perpendicular to the x' axis in the orbital plane.

The IMAGE spin vector points opposite to the z axis, and therefore the voltages in the primed coordinate system are

$$V_{x'} = V_x \cos 2\pi S t' + V_y \sin 2\pi S t'$$
  

$$V_{y'} = -V_x \sin 2\pi S t' + V_y \cos 2\pi S t'$$
  

$$V_{z'} = V_z$$
  
(5.1-2)

Here  $V_x$ ,  $V_y$ ,  $V_z$  are the corrected voltages in the antenna coordinate system, S is the spin rate (S = 1/120 sec), and t' is the time measured from the last alignment of the x axis with the x' axis.

#### 5.1.7 Digital signal processing

Certain RPI waveforms require specialized onboard signal processing. The processing includes pulse compression for the complementary phase code sequences, and spectral analysis for equidistant pulse sequences. For the purpose of calibration and conversion of amplitudes to physical units, it is important that the "digital" gain of the signal processing is known.

#### 5.1.8 Linear-to-log signal compression

In order to reduce the telemetry data volume, some of the output data are converted to amplitude/phase representation and logarithmically compressed. The amplitude  $A_{\text{lin}}$  and phase  $\phi$  can be obtained from the in-phase and quadrature samples *I* and *Q* using equation (5.1-3):

$$A_{lin} = \sqrt{I^2 + Q^2}$$

$$\varphi = \operatorname{arctg}\left(\frac{Q}{I}\right)$$
(5.1-3)

The phase  $\varphi$  is then stored in an 8-bit integer, in linear 360°/255 steps. The amplitude  $A_{\text{lin}}$  is converted to the logarithmic scale and stored in another 8-bit integer:

$$A_{\log} = 20 \log_{10}(A_{lin}) \cdot C_1 + C_2 \tag{5.1-4}$$

The constants  $C_1$  and  $C_2$  are selected to accommodate the dynamic range of  $A_{\text{lin}}$  in the 256 levels of  $A_{\text{log}}$ . The choice of  $C_1$  and  $C_2$  is influenced by the need to minimize real-time computations. By rewriting (3.1-4) as

$$A_{\log} = \left[10\log_{10}\left(I^{2} + Q^{2}\right)\right] \cdot C_{1} + C_{2}$$
(5.1-5)

the root function does not have to be calculated. Also,  $log_2()$  function can be used instead of a slower implementation of  $log_{10}()$ :

$$A_{\log} = 10 \frac{\log_2 (I^2 + Q^2)}{\log_2 10} \cdot C_1 + C_2 = 3.0103 \ \log_2 (I^2 + Q^2) \cdot C_1 + C_2$$
(5.1-6)

C<sub>1</sub> shall be then selected to allow enough dynamic range. The 12-bit digitizer produces 12 bit numerical voltage values (11 bits and sign) for *I* and *Q*. Assuming that both *I* and *Q* are saturated, the maximum  $A_{\text{lin}}$  is  $(2^{11}-1) \cdot \sqrt{2}$ . For 4, 8, and 16 chip phase code waveforms, the pulse compression processing (Section 3.1.7) increases the maximum amplitude 4, 8, and 16 times, correspondingly, resulting in  $(2^{13}-1) \cdot \sqrt{2}$ ,  $(2^{14}-1) \cdot \sqrt{2}$ , and  $(2^{15}-1) \cdot \sqrt{2}$  values of the maximum  $A_{\text{lin}}$ . Therefore, the maximum amplitude to be ever converted to log scale is  $32767 \cdot \sqrt{2} = 46340 = 93.32$  dB. Making

$$C_1 = \frac{8}{3.0103} \tag{5.1-7}$$

allows for  $255 \cdot 3.0103/8 \approx 96$  dB dynamic range of  $A_{log}$  and a convenient formula for  $A_{log}$  calculation:

$$A_{\log} = 8 \log_2 (I^2 + Q^2) + C_2$$
(5.1-8)

To simplify the ground processing,  $C_2$  is selected to always reference the maximum possible value of  $A_{\text{lin}}$ , for each waveform, to the maximum level of  $A_{\text{log}}$  (i.e., 255):

$$C_{2} = C_{3} - C_{4}$$

$$C_{3} = 72.547$$
(5.1-9)
$$C_{4} = \begin{cases} 64, & \text{for } 16 - \text{chip code} \\ 48, & \text{for } 8 - \text{chip code} \\ 32, & \text{for } 4 - \text{chip code} \\ 0, & \text{for all other waveforms} \end{cases}$$

Shifting of the reference level by introducing the waveform-dependent  $C_4$  constant normalizes the DSP gain from the pulse compression (Section 5.1.7) and thus simplifies the log-to-linear decompression algorithm discussed below in the Section 5.2.2.1.

#### 5.2 Converting RPI readings to physical units

Table 5.2-1 shows the choice of physical units for the RPI science data.

Measured parameter	Standard units	Stored in the data as	Calibration/Conversion
Nominal Frequency	KHz	Frequency Step Number	Section 2.4.1
Range	Km	Range Bin Number	Section 3.2.1
Field Strength	nVp/m*	12 bit quadrature component	Section 3.2.2
Field Strength	nVp/m*	8 bit log amplitude, except TTD databin	Section 3.2.2
Voltage	dBV/root-Hz	8 bit log amplitude (TTD databin)	Section 3.2.3
Antenna voltage	Vrms	8 bit values in Frequency Header	Section 3.2.6
Antenna current	MA	8 bit values in Frequency Header	Section 3.2.6
Phase	Degrees	8 bit linear phase	Section 3.2.4
Doppler Frequency	Hz	Doppler Bin Number	Section 3.2.5

 Table 5.2-1
 Physical units for RPI science data

#### 5.2.1 Converting range bin number to km

The range bin number,  $\tilde{r}$ , for a particular databin is obtained using Equation 3.2-4, Section 3.2.3. Then the range in km is

$$R = [E] \cdot 960 + (\tilde{r} + r_{st}) \cdot 10[H]$$
(5.2-1)

where

[E]	is Start Range in 960 km units (from Preface)
$\widetilde{r}$	is range bin number
r <sub>st</sub>	is First Range Bin (from Frequency Header, Table 4.2-7)
[H]	is Range Resolution in 10 km (from Preface), i.e., 24 or 48

<sup>\*</sup> RPI received voltages are defined as peak-to-ground, not rms. Vp corresponds to the amplitude of the phasors (the arrows shown in Figure 3.1-3).

\_\_\_\_\_

#### 5.2.2 Converting amplitude to field strength in $[^{nVp}/_{m}]$

Figure 5.2-5 details the ground processing steps to convert measured amplitudes from the raw telemetry representation to the field strengths in  $[{}^{nVp}/{}_m]$ . Onboard calibration tables used by the flight software v31 and below have to be replaced by an updated calibration data now available. Before the calibration corrections to the quadrature samples can be removed, un-despinning of the data has to be done. After the new corrections are introduced, despinning has to be reapplied.

#### 5.2.2.1 Log-to-linear decompression

RPI science data with databin formats SSD, SMD, PRD, SBD and DBD (see Section 3.2) report 8 bit logarithmically compressed amplitudes. The amplitudes have to be converted back to linear scale before they enter the rest of the conversion process:

$$A_{lin} = 10^{\frac{A_{log} - C_3}{20C_1}}$$
(5.2-2)

where  $A_{log}$  is the stored amplitude, and  $C_1$  and  $C_3$  are the compression algorithm constants:

$$C_1 = \frac{8}{3.0103}$$
(5.2-3)  
$$C_3 = 72.547$$





#### 5.2.2.2 Polar to Rectangular Conversion

For spectral domain data, the in-phase and quadrature components are restored from the amplitude and phase:

$$I = A_{lin} \cos \varphi$$

$$Q = A_{lin} \sin \varphi$$
(5.2-4)

where  $\phi$  is the phase in radians obtained from the 8-bit stored value as discussed below in Section 5.2.4.

#### 5.2.2.3 Un-despinning

The de-spinning procedure (Section 5.1.6) has to be undone before the v28 corrections can be removed. The rotation is done in the opposite direction to de-spinning (5.1-2):

$$V_{x} = V_{x'} \cos 2\pi S t' - V_{y'} \sin 2\pi S t'$$
  

$$V_{y} = V_{x'} \sin 2\pi S t' + V_{y'} \cos 2\pi S t'$$
(5.2-5)

 $V_x$  and  $V_y$  are the voltages in the antenna coordinate system, *S* is the spin rate (1/120 sec), and *t*' is the time measured from the last alignment of the *x* axis with the *x*' axis. For all time domain data, *t*' is the time offset from the nadir,  $\Delta T_{nadir}(f)$ , stored in Data Header of each telemetry packet. If more than one frequency data fits one packet,  $\Delta T_{nadir}(f)$  for the second, third,... frequency of the packet has to be interpolated (or extrapolated, for the last packet). For the spectral domain data, 0.5 CIT has to be added to *t*' (see Section 5.2.5 for CIT calculation). Spin rate magnitude *S* is stored in the Preface.

#### 5.2.2.4 Un-scaling

All X and Y channel data had been scaled down by a factor of 8 for the purpose of optimal binary data storage (see Section 5.1.5). This factor has to be removed here by multiplying the amplitudes by 8.

#### 5.2.2.5 Removing correction factors

Only amplitude corrections for the flight software v31 and below have to be removed, so the un-calibration procedure is simply:

$$Q_{x,y} = \frac{Q_{xc,yc}}{A_{xc,yc}}$$

$$I_{x,y} = \frac{I_{xc,yc}}{A_{xc,yc}}$$
(5.2-6)

where  $A_{xc}$  and  $A_{yc}$  are the amplitude corrections introduced by the flight software. The onboard correction factors are reported in the calibration packet as 8-bit log-scale amplitudes and 8-bit phases for the channels X, Y, and Z.  $A_{xc}$  and  $A_{yc}$  can be restored from CAL packet data using the following formula:

$$A_{xc,yc} = \frac{2 \cdot 8}{1000\sqrt{2}} 10^{\frac{CAL_{x,y} - 72.547}{53.151}} = 0.0113137 \cdot 10^{\frac{CAL_{x,y} - 72.547}{53.151}}$$
(5.2-7)

where  $CAL_x$  and  $CAL_y$  are the calibration amplitudes of X and Y channels.

#### 5.2.2.6 Re-calibrating

Re-calibration involves amplitude scaling only, and therefore can be expressed simply as

$$Q'_{xc,yc} = Q_{x,y} \cdot A'_{xc,yc}$$

$$I'_{xc,yc} = I_{x,y} \cdot A'_{xc,yc}$$
(5.2-8)

The table with the new amplitude correction factors  $A'_{xc}$  and  $A'_{yc}$  can be found in Appendix C, Table C1-1.

#### 5.2.2.7 Despinning

The de-spinning procedure (Section 5.1.6) has to be done after the new corrections are applied, using the equations (5.1-2) and the offset time *t*' from Section 5.2.2.3.

#### 5.2.2.8 Applying coefficients from the Physical Units Table

The Physical Units Table Each table has coefficients  $C_{x,y,z}(f, [G])$  in [nV/unit] for all settings of base gain [G] and selected set of frequencies. The table is derived from the Z channel calibration results obtained during the amplitude calibration at [G] = 15 (see description of the calibration in Appendix C and the coefficient values in Table C3-1). The coefficients for other settings of [G] are obtained using the relative gain data shown in Table 5.1-1:

$$C_{x,y,z}(f,[G]) = C_{x,y,z}(f,15) \cdot 10^{\frac{C_{x,y,z}(f,15) - C_{x,y,z}(f,[G])}{20}}$$

$$C_{x,y}(f,15) = C_{z}(f,15)$$
(5.2-9)

#### 5.2.2.9 Calculations of field strength

The received field strength,  $E_{\rm R}$ , is proportional to the antenna voltage, V:

$$\vec{E}_R = \frac{1}{\vec{L}'}\vec{V} \tag{5.2-10}$$

where the proportionality factor L' is the effective antenna length,  $L' \approx 0.5L_a$ ,  $L_a$  is the tip-totip dipole length. The effective antenna lengths are

$$L'_{X} = L'_{Y} = 250m$$

$$L'_{Z} = 10m$$
(5.2-11)

#### 5.2.3 Converting thermal noise amplitudes to [ dBVrms/root-Hz]

The processing steps to convert thermal noise amplitudes from the raw telemetry representation to  $\left[\frac{dBV(rms)}{root-Hz}\right]$  are shown in Figure 5.2-6.



#### Figure 5.2-6 Physical units conversion for thermal noise data

Logarithmic compression of TTD amplitudes is done differently from the spectral domain data (see Appendix A). To convert TTD amplitudes to the linear scale, the following formula is used:

$$A_{lin} = 10^{\frac{1}{\ln(10)}(A_{log}+9.031)-9.031}_{20}$$
(3.2-12)

Un-scaling, un-calibrating, re-calibrating and conversion to nVp is done the same way it is done for other databins. Then nVp are converted to  $V_{rms}$ , and then the thermal noise energy collected over the receiver bandwidth of 300 Hz is normalized to 1 Hz, which corresponds to  $1/\sqrt{300}$  factor in voltage. Finally, the value is put in dB scale.

#### 5.2.4 Converting phase data to physical units

All phase values given in the RPI data can be converted from 8 bit integer number to 1° units by multiplying them with 360/255.

#### 5.2.5 Converting Doppler bin number to Hz

The coherent integration time is

$$T = \frac{2^{[N]_a} \cdot [S]'}{[R]'} , [s]$$
(3.2-13)

 $[N]_{a}$  is absolute value of Number of Repetitions

[S]' is the Number of Fine Steps, [S], only if it is a positive value, 1 otherwise

[R]' is Pulse Repetition Rate in pps units; when [R] from Preface is 0, [R]' is 0.5

The Doppler frequency increments are

$$\Delta d = \frac{1}{T}, \quad [\text{Hz}] \tag{3.2-14}$$

The Doppler frequencies corresponding to the Doppler bin numbers are listed in Table 5.2-2.

[N]	Doppler bin	Doppler frequencies, Hz
	numbers	
0	1	N/A
1	1-2	$-\frac{1}{2}\Delta d$ , $+\frac{1}{2}\Delta d$
2	1-4	$-{}^{3}/{}_{2}\Delta d, -{}^{1}/{}_{2}\Delta d, +{}^{1}/{}_{2}\Delta d, +{}^{3}/{}_{2}\Delta d$
3	1-8	$-\frac{7}{2}\Delta d$ , $-\frac{5}{2}\Delta d$ ,, $-\frac{1}{2}\Delta d$ , $+\frac{1}{2}\Delta d$ , $+\frac{5}{2}\Delta d$ , $+\frac{7}{2}\Delta d$
4	1-16	$-\frac{15}{2}\Delta d, -\frac{13}{2}\Delta d, \dots, -\frac{1}{2}\Delta d, +\frac{1}{2}\Delta d, \dots +\frac{13}{2}\Delta d, +\frac{15}{2}\Delta d$
5	1-32	$-{}^{31}/_2\Delta d, -{}^{29}/_2\Delta d, \dots, -{}^{1}/_2\Delta d, +{}^{1}/_2\Delta d, \dots +{}^{29}/_2\Delta d, +{}^{31}/_2\Delta d$
6	1-64	$-\frac{63}{2}\Delta d, -\frac{61}{2}\Delta d, \dots, -\frac{1}{2}\Delta d, +\frac{1}{2}\Delta d, \dots +\frac{61}{2}\Delta d, +\frac{63}{2}\Delta d$
7	1-128	$-\frac{127}{2\Delta d}, -\frac{125}{2\Delta d}, \dots, -\frac{1}{2\Delta d}, +\frac{1}{2\Delta d}, \dots +\frac{125}{2\Delta d}, +\frac{127}{2\Delta d}$

Table 5.2-2Doppler shift frequency

#### 5.2.6 Converting antenna impedance data to physical units

Frequency Header contains six 8-bit values from the antenna impedance measurement:

Measured characteristic	Physical	Conversion Polynomial
	Units	
Current on X antenna [Ix]	mA	0.017196*x <sup>2</sup> +23.697063*x+18.055805
Voltage on +X dipole antenna $[V_{x1}]$	V(r.m.s)	$0.001041*x^3-0.079089*x^2+6.833423*x+77.628601$
Voltage on -X dipole antenna $[V_{x2}]$	V(r.m.s)	$0.000340^{*}x^{3}$ - $0.072471^{*}x^{2}$ + $10.139749^{*}x$ + $27.581501$
Current on Y antenna [Iy]	mA	0.021766*x <sup>2</sup> +21.881399*x+15.814330
Voltage on +Y dipole antenna $[V_{y1}]$	V(r.m.s)	0.041969*x <sup>2</sup> +3.503154*x+96.108014
Voltage on =Y dipole antenna $[V_{y2}]$	V(r.m.s)	0.039404*x <sup>2</sup> +3.459442*x+96.996135

Table 5.2-3 Antenna impedance data in physical units

## **RPI Level 0 House Keeping Data** Formats

The following sections introduce and describe the formats for housekeeping (HK) data produced by the RPI instrument, which include R\_HK Housekeeping packet with Build-In Test results, R\_SRD Segment Report packet containing the contents of RPI SRAM segments, R\_MSG Software Message packet containing software generated message, and R\_ECH Command Echo packet with a copy of the latest ground command.

#### 6 HOUSE KEEPING DATA

There are four RPI housekeeping (HK) data packets reporting various information pertaining to instrument operations. All HK packets include the standard CCSDS data header, followed by HK Header, Data Block whose content depends on the type of HK information, and a checksum as shown in Table 5.2-1.

<i>Table 5.2-1</i>	Universal RPI	Housekeeping	packet format
--------------------	---------------	--------------	---------------

Sec 4.2.1	Sec 6.1	Sec 6.2-6.5	Sec 4.2.7
CCSDS Preamble	HK Header	Data Block	Checksum

#### 6.1 Housekeeping Header

Housekeeping Header format is identical to all four HK packets (R\_HK, R\_SRD, R\_MSG, and R\_ECH). It contains five items, as shown in Table 6.1-1.

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
7	0	1	Packet ApID	N/A	N/A
8	1	1	Software version	N/A	0-255
912	25	4	CIDP MET stamp	0.1 sec	0 to 4294967296
1316	69	4	RPI MET stamp	0.1 sec	0 to 4294967296
1718	1011	2	Argument of perigee	LSB=5.5* 10 <sup>-3</sup>	0 to 360

#### Table 6.1-1 HK Header

Packet ApID is preserved for data identification purpose outside the standard data archive environment. Software version is reported for backward compatibility in case of design changes. CIDP and RPI time stamps are given for the clock comparison purpose. Orbital position phase is given to verify calculation algorithm.

#### 6.2 (R\_HK) House Keeping data sets. ApID = 0x02

The RPI house keeping represents the RPI health and safety data packet. The R\_HK packet is generated by RPI to report on system (hardware and software) status. The packet is sent periodically (nominally every 10 minutes) or by request from the ground. The structure of the data block is given in subsequent sections. Each section describes part of the data block that is given by the overview in Table 6.2-1.

Sec 4.2.1	Sec 6.1	Sec 6.1 Sec 6.2.1 Sec 6.2.2 Sec 6.2.3 Sec 6.2.4 Sec 6.2.5 Sec 6.2.5							
Data	HK	Misc.	Digital	Analog	NoGo	Power	Checksum		
Packet	Header	status info	Sensors	Sensors	Table	Limits			
Preamble									

#### Table 6.2-1 RPI House Keeping data format

#### 6.2.1 Miscellaneous status information

This section contains various status information items listed in Table 6.2-2.

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
1922	0	4	Last SST in the SST Queue	0.1 sec	0 to 4294967296
23	4	1	Memory checksum failure	N/A	01, 1 -failed
24	5	1	Program status (format variable)	N/A	0-255
25	6	1	Communication Status (from serial port UART)	N/A	0-255

Table 6.2-2Miscellaneous status information

#### 6.2.2 Digital Sensor Readings

This section contains digital sensor readings in accordance with the state of digital I/O lines on the BIT card.

Table 6.2-3 Digital sensor readings

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
26	0	1	Digital sensor readings	N/A	0-255

Each bit of the status byte signifies if reading is valid or not valid. The actual bit readings need to be compared against the expected "Go" value to correctly interpret the result. This comparison is done onboard to fill the NoGo Table where 1 always indicates "NoGo" (and 0 indicates "Go").

The Digital Sensors names and "Go" condition are listed in Table 6.2-4. The following categories of signals are monitored:

• 16MHz RPI master 16 MHz oscillator signal

•	Vc	Antenna coupler voltages +12 and +24V

• V DC -5, -15 and +15V

Table 6.2-4 Di	gital Sensor	Readings
----------------	--------------	----------

	D7	D6	D5	D4	D3	D2	D1	D0
Signal name	-	16 MHz	+24 Vc	-	+12Vc	-5V	-15 V	+15 V
GO condition	-	1	1	-	1	0	0	1

Go conditions for digital sensors are specified in the onboard ARMENU control structure, question 351 (see *RPI Commanding* document, Section 2).

#### 6.2.3 Analog Sensor Readings

This section contains the measurements from the analog input channels on the BIT card. The values are 16 bit integers with 12 bits containing raw value from the ADC.

Byte Count Offset	Byte Offset No	Byte Length	Description	Туре	Units	Range
2728	01	2	Channel.00 Xmtr Xb	В	5/4096 V	0-2.5 V
2930	23	2	Channel.01 Xmtr Yb	В	5/4096 V	0-2.5 V
3132	45	2	Channel.02 1st Lob	В	5/4096 V	0-2.5 V
3334	67	2	Channel.03 SysTemp	S	5/4096 V	0-2.5 V
3536	89	2	Channel.04 500 kb	В	5/4096 V	0-2.5 V
3738	1011	2	Channel.05 3.84 Mb	S	5/4096 V	0-2.5 V
3940	1213	2	Channel.06 95 kb	S	5/4096 V	0-2.5 V
4142	1415	2	Channel.07 X+Tmp	В	5/4096 V	0-2.5 V
4344	1617	2	Channel.08 X-Tmp	В	5/4096 V	0-2.5 V
4546	1819	2	Channel.09 Y+Tmp	S	5/4096 V	0-2.5 V
4748	2021	2	Channel.10 Y-Tmp	S	5/4096 V	0-2.5 V
4950	2223	2	Channel.11 Ztmp	S	5/4096 V	0-2.5 V
5152	2425	2	Channel.12 RFX+	В	5/4096 V	0-2.5 V
5354	2627	2	Channel.13 RFX-	В	5/4096 V	0-2.5 V
5556	2829	2	Channel.14 RFY+	В	5/4096 V	0-2.5 V
5758	3031	2	Channel.15 RFY-	В	5/4096 V	0-2.5 V
5960	3233	2	Channel.16 RFSmpZ	В	5/4096 V	0-2.5 V
6162	3435	2	Channel.17 RFSmpX	В	5/4096 V	0-2.5 V
6364	3637	2	Channel.18 IFSmpZ	В	5/4096 V	0-2.5 V
6566	3839	2	Channel.19 IFSmpY	В	5/4096 V	0-2.5 V
6768	4041	2	Channel.20 2500 b	S	5/4096 V	0-2.5 V
6970	4243	2	Channel.21 400 kb	S	5/4096 V	0-2.5 V
7172	4445	2	Channel.22 XvarI	В	5/4096 V	0-2.5 V
7374	4647	2	Channel.23 YvarI	В	5/4096 V	0-2.5 V
7576	4849	2	Channel.24 YvarV	В	5/4096 V	0-2.5 V

Table 6.2-5 Analog sensor readings

Type B = Burst measurement of a pulse signal must be done during sounding only.

Type S = Single measurement of a continuous signal may be done anytime.

#### 6.2.4 NoGo Table

This section contains 5 bytes indicating Go/NoGo condition of all sensor readings. Each bit of the NoGo Table bytes is set to 1 (NoGo) if:

- analog sensor reading is outside the onboard red tolerance limits or digital sensor reading is not GO and
- the sensor is specified as capable of generating NoGo condition.

Onboard red limits are specified in questions 330-343 of the ARMENU control structure (see *RPI Commanding* document, section 2.1), GO conditions of digital sensors are given in question 351 of the ARMENU structure, and sensors capable of generating NoGo condition are listed in questions 361-365.

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
77	0	1	Digital Sensor	N/A	0-255
78	1	1	Analog Status : Ch00-Ch07	N/A	0-255
79	2	1	Analog Status : Ch08-Ch15	N/A	0-255
80	3	1	Analog Status : Ch16-Ch23	N/A	0-255
81	4	1	Analog Ch24 and Reserved Bits	N/A	0-255

 Table 6.2-6
 NoGo Table

The Digital and Analog sensor flags and their associated reading parameters are listed in Table 6.2-7.

Line	Category	D7	D6	D5	D4	D3	D2	D1	D0
Count									
0	Byte 1	-	16 MHz	+24 Vc	_	+12Vc	-5V	-15 V	+15 V
	digital								
4	Ch00-Ch07	XMTR 1	XMTR 2	1 <sup>st</sup> LO	SysTem	C140K	3.84M	95kHz	X+tmp
	analog.				р		Hz		
5	Ch08-Ch15	X-tmp	Y+tmp	Y-tmp	Ztmp	RFX+	RFX-	RFY+	RFY-
	analog.								
6	Ch16-Ch23	RFSmpZ	RFSmpX	IFSmpZ	IFSmpX	2500	400	XvarI	YvarI
	analog.			_	_	Hz	kHz		
7	Reserved	XyvarV	Reserved						

Table 6.2-7 Digital and Analog sensor flag parameters

#### 6.2.5 RPI Power Limits

If necessary, PRI can be instructed to use power limit different from the limit specified in the measurement programs (see program parameter 11(W) in the Preface, Section 4.2.3). There is a pass-through command R\_SYS\_PLIM\_SET that specifies Peak and Average power limits. Before running a program, RPI evaluates all available limits, and selects the minimum.

#### UMLCAR RPI Telemetry Data Model v 2.8

The following section of HK packet reports current settings of peak and average power limits as instructed from the ground.

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
82	0	1	Peak Power Limit	Watts	0-255
83	1	1	Average Power Limit	Watts	0-255

Table 6.2-8 Peak and Average Power Limits

#### 6.3 (R\_SRD) Segment Report data set. ApID=0x04

This report segment is generated by RPI in response to the ground request R\_MEM\_DATA\_SEND, which instructs RPI to downlink a specific segment of memory from the RPI CPU. The segment can be a section of the flight software or one of the control data structures (Programs, Schedules, SST Tables, ARMENU). The structure of the Segment Report packet is given in Table 6.3-1.

 Table 6.3-1
 RPI Segment Report data format

	RPI-SRD F		
Sec_4.2.1	Sec_6.1	Sec_6.3.1	Sec_4.2.7
Data Packet	НК	Segment data	Checksum
Preamble	Header		

#### 6.3.1 Segment Data

Data Packet

The segment data are stored in accordance to the format described in Table 6.3-2.

#### Table 6.3-2Segment Data

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
1920	01	2	SCLen Segment length	N/A	0-65536
2124	25	4	Segment Address	32 bit words	0-0x00FFFFFF
25SCLen*4+25	3SCLen*4+3	SCLen*4	Segment Contents	N/A	N/A

#### 6.4 (R\_MSG) Software Message. ApID=0x06

ΗK

When a software fault is detected, a R\_MSG software message packet is generated. The message contains a message code (associated with a table for identification of the problem type), and two message parameters. The structure of the Software Message packet is given in Table 6.4-1.

		RPI-MSG Block	
Sec 4.2.1	Sec 6.1	Sec 6.4.1	Sec 4.2.7

Software message

Table 6.4-1	<b>RPI</b> Segment	Report dat	a format
	ILL I DOGINOUN	Lepoir www	

Checksum

Preamble Header	
-----------------	--

#### 6.4.1 Software Message

#### Table 6.4-2Software message

Byte Count Offset	Byte Offset	Byte Length	Description	Units	Range
19	0	1	Message Code	Table 7.1-2	0-255
2023	14	4	Message Parameter #1	Table 7.1-2	Message dependent
2427	58	4	Message Parameter #2	Table 7.1-2	Message dependent

Message codes and the associated parameters are listed in Table 6.4-3.

Table 6.4-3	Message	Codes and	<b>Parameters</b>
-------------	---------	-----------	-------------------

Message		Message Code Description	Message Parameters Description	
Code				
202	0xCA	CIT start timeout	#1 Timeout, sec	
203	0xCB	Pulse start timeout	#1 Timeout, sec	
204	0xCC	Prerun condition timeout	#1 Timeout, sec	
205	0xCD	Blank command parameter	#1 Command stem	
207	0xCF	No timing port signal		
208	0xD0	No 1_PPS signal		
209	0xD1	No Clock Pulse signal		
210	0xD2	Digitizer timeout	#1 Timeout, sec	
211	0xD3	EEPROM load error		
212	0xD4	EEPROM save error	#1 Address, 32 bit	
213	0xD5	Data upload checksum error	#1 Checksum, 8 bit	
214	0xD6	Bad command stem	#1 Command stem	
215	0xD7	System is not in HiPower to execute command		
216	0xD8	Communications: Unknown Error		
217	0xD9	Communications: Framing Error		
218	0xDA	Communications: Sync. Byte Error		
219	0xDB	Communications: Bad Command Message Checksum		
220	0xDC	Communications: Bad Command Message Header		
221	0xDD	Communications: Bad Command Stem		
222	0xDE	Communications: Bad Upload Checksum		
223	0xDF	Communications: Bad Upload Address		
224	0xE0	Communications: Command Queue Overflow		
225	0xE1	SST Queue Overflow		
226	0xE2	SST Queue Error: MET Already Active		
227	0xE3	SST Queue Error: MET already passed		
228	0xE4	Bad CIDP Data Block Number in Data Load Request		
229	0xE5	Lost Sync. Pulse (Delphi)		

#### 6.5 (R\_ECH) Command Echo. ApID=0x08

Every command sent to RPI has a corresponding RPI\_ECHO packet sent back as an acknowledgement. The structure of the Software Message packet is given in Table 6.5-1.

#### Table 6.5-1 RPI Command Echo format

	R_ECH B		
Sec_4.2.1	Sec_6.1	Sec_6.5.1	Sec_4.2.7
Data Packet	НК	Command Replica	Checksum
Preamble	Header		

#### 6.5.1 Command Replica

Byte Count Offset	Byte Offset No	Byte Length	Description	Units	Range
19	0	1	Command stem	N/A	0-255
2023	1	4	Command action Parameter 1	N/A	Command specific
2427	5	4	Command action Parameter 2	N/A	Command specific

#### Table 6.5-2 Command Replica

47

## **RPI Development Packet Formats**

The following sections introduce and describe the formats for development data packets produced by the RPI instrument in response to debugging commands.

#### 7 Development Packet Formats

RPI responds to certain development commands by outputting Development Packet(s) to the RS-422 port (to be received by CIDP, GSEOS, ASIST, etc.). All development packets are formatted as standard Science Data Packets, however, they are unlikely to be used during the mission time.

#### 7.1 ApID=0x1F Frequency Set Response Packet

The frequency set command R\_DEB\_FREQ\_SET is acknowledged by a message giving the programmed frequency, the coupler mode character, the relay settings for all four couplers, the synthesizer control byte settings, and the preselector control byte setting (see Table 7.1-1).

Byte No.	Name	Value	Comments
02	Sync pattern	FEFA30h	
3	Header	0xDC	Data packet
4	ApID	0x1F	
56	Byte Count	21	(constant)
7-10	Frequency	f<31:24>	
		f<23:16>	Sounding frequency in Hz.
		f<15:8>	
		f<7:0>	
11	Coupler mode	'N' - normal	This character indicates whether a special coupler mode
		'D' - direct	has been selected.
		'C' - calibrate	
		'S' - calibrate-direct	
1213	Xplus relays	<15:8>	This 16-bit value indicates the states of the 16 relays in
		<7:0>	this antenna coupler. Bit zero equals 1 if relay K1 is on;
			bit 1 is 1 for relay K2, etc.
1415	Xminus relays	<15:8>	This 16-bit value indicates the states of the 16 relays in
		<7:0>	this antenna coupler. Bit zero equals 1 if relay K1 is on;
			bit 1 is 1 for relay K2, etc.
1617	Yplus relays	<15:8>	This 16-bit value indicates the states of the 16 relays in
		<7:0>	this antenna coupler. Bit zero equals 1 if relay K1 is on;
			bit 1 is 1 for relay K2, etc.
1819	Yminus relays	<15:8>	This 16-bit value indicates the states of the 16 relays in
		<7:0>	this antenna coupler. Bit zero equals 1 if relay K1 is on;
			bit 1 is 1 for relay K2, etc.

 Table 7.1-1
 Frequency Set Response packet, ApID=0x1F

20	Reg5			LO freq = Reg5*125 kHz	
21	Reg4		Synth.	+ Reg4*125 khz / 2 <sup>8</sup>	
22	Reg3		Control	$+ \text{Reg3*125 kHz} / 2^{16}$	
23	Reg2		Registers $+ \text{Reg2*125 kHz} / 2^{24}$		
24	Reg1		+ Reg1*125 kHz / 2 <sup>32</sup>		
25	Reg0			$+ \text{Reg0*125 kHz} / 2^{40}$	
26	Data Byte "n"	pfrq	Preselector control byte		
27	Checksum		xor sum bytes 7-26		

#### 7.2 ApID=0x2F Memory Read/Write Response Packet

The memory read/write command reply gives the starting and ending addresses of the memory block followed by the contents of the block. The format for the memory read/write command reply message is given in Table 7.2-1.

Table 7.2-1 Memory Read/Write Response packet, ApID=0x2F

Byte No.	Name	Byte Value	Comments	
02	Sync pattern	FEFA30h		
3	Header	0xDC	Data packet	
4	ApID	0x2F		
56	Byte Count		Byte $Cnt = 10 + 4*(Addr2-Addr1+1)$	
7	Data Byte 0	'R' or 'W'	'R' = memory block read, 'W' = memory block write	
811	Starting Address	<31:24> <23:16> <15:8> <7:0>	Starting address of memory block to be read/written	
1215	Ending Address	<31:24> <23:16> <15:8> <7:0>	Ending address of memory block to be read/written	
1619	Data 1	<31:24> <23:16> <15:8> <7:0>	32 bit word	
15+4*n		Checksum	xor sum bytes 7-19	

#### 7.3 ApID=0x3F VME Read/Write Response Packet

The VME Read/Write response packet returns the VME address and contents for the affected VME port. The format for the VME read/write command reply message is given in Table 7.3-1.

Byte No.	Name	Byte Value	Comments
02	Sync pattern	FEFA30h	
3	Header	0xDC	Data packet
4	ApID	0x3F	

Table 7.3-1 VME Read/Write Response packet, ApID=0x3F

49

56	Byte Count	6	
710	Address	<31:24> <23:16> <15:8> <7:0>	VME Address of affected VME port
11	Value		Contents of affected VME port after VME Port command is executed.
12	Checksum		xor sum bytes 7-11

#### 7.4 ApID=0x4F Digitizer Samples Packet

The R\_DEB\_DGTZ\_GET command continuously takes digitizer samples, sending back digitizer sample blocks as indicated below. Packets are transmitted continuously until RPI receives a new command. The format for the Digitizer Samples packet is shown in Table 7.4-1.

**Byte** Name **Byte Value** Comments No. 0..2 Sync pattern FEFA30h 3 Header 0xDC Data packet 4 ApID 0x4F Byte Count 4N+1 N = number of complex samples 5..6 Real 1 First real sample 7..8 <15:8> <7:0> 9..10 Imaginary 1 <15:8> First imaginary sample <7:0> 11..12 Real 2 <15:8> Second real sample <7:0> 13..14 Imaginary 2 Second imaginary sample <15:8> <7:0> . . . . . . Real N <15:8> Nth real sample <7:0> Nth imaginary sample Imaginary N <15:8> <7:0> 4N+6 Checksum xor sum

Table 7.4-1	Digitizer	Sample	nacket.	ApID=0x4F
1 4010 7.4-1	Digniter	Sumpic	pucker,	InpiD-0AH

#### Appendix A. Thermal Noise Data Processing

Since lots of effort has been put into making standard reusable tools for operational software and data analysis software we would like to find a way to structure the TTD output telemetry packets to use the standard RPI packet format (see Section 2). In order to force TTD data into this format, a TTD databin has to be introduced. In the thermal noise mode, RPI produces averaged amplitudes (for each antenna), as well as cross-power and cross-phase terms for each 8 average amplitudes (see Section 1.1 for more details). To avoid paying too dearly in storage efficiency, we have defined the standard TTD databin with 8x3 average amplitudes, 3 cross-power terms, and 3 cross-phase terms, thus making N=3 the minimum value allowed. This requires that we have at least 36 time domains samples per frequency step<sup>2</sup>.

The elements of the TTD databin are 8-bit Logarithmic amplitudes, 8-bit cross-power log amplitudes, and the corresponding cross-power phase arguments also in an 8-bit format (0-359 deg in 1.4deg steps). The algorithm for computing one databin elements uses 36 samples collected on each of three antennas ( $S_{x1}$  to  $S_{x36}$ ,  $S_{y1}$  to  $S_{y36}$ , and  $S_{z1}$  to  $S_{z36}$ ).

#### A1. Calculating Log Amplitudes

The goal is to compute 8-point average amplitudes in the logarithmic scale. For the sake of computational efficiency, calculations operate with the power terms. The signal power terms for antenna X,  $p_{xi}$ , can be obtained from the complex samples  $S_i$ :

$$p_{xi} = I_{xi}^2 + Q_{xi}^2, \ i = 1..8 \tag{A-1}$$

where  $I_{xi}$  is the real (in-phase) component of the sample  $S_i$ , and  $Q_{xi}$  is the imaginary (quadrature) component of  $S_i$ . Note that the power term is always positive, so we can add the terms without concern that anti-phased signals may cancel each other:

$$P_{x} = \sum_{i=1}^{8} p_{xi}$$
 (A-2)

Averaging and converting to log scale gives the first average amplitude  $A_x$ :

$$A_{x}[1] = 10\log_{10}\left(\frac{P_{x}}{8}\right) = 10\log_{10}P_{x} - 10\log_{10}8 = 10\log_{10}P_{x} - 9.031$$
(A-3)

Now move the starting point up 4 samples, and create a new 8-point average which overlaps half the data used in the previous average. Continue up until samples 29 to 36 are used in making the eighth average, the final amplitude to store in the TTD databin.

 $<sup>^{2}</sup>$  For standard sounder modes, all of samples are collected after a single pulse. The TTD mode is a Receive Only mode, so there is no transmitted pulse, but there is still a logic pulse that triggers the digitizer to make a one-dimensional sample array of 32 to 1024 samples at each frequency step.

Repeat for  $A_y[1-8]$  and  $A_z[1-8]$ . Store all  $A_{x,y,z}[1]$  to  $A_{x,y,z}[8]$  (24 values) in the databin.

#### A2. Calculating Cross Power Terms (XY, XZ and YZ)

Three complex cross-power terms,  $W_{xy}$ ,  $W_{yz}$ , and  $W_{xz}$ , can be calculated from the samples obtained simultaneously from antenna X, Y, and Z:

$$W_{xy} = (I_x + j Q_x) * (I_y - j Q_y)$$
 (A-4)

$$W_{xz} = (I_x + j Q_x) * (I_z - j Q_z)$$
 (A-5)

$$W_{\rm yz} = (I_{\rm y} + j Q_{\rm y}) * (I_{\rm z} - j Q_{\rm z})$$
(A-6)

Conjugating the Y sample in (A-4) gives the cross-power vector,  $W_{xy}$ , a phase equal to the phase difference between the X axis and Y axis sample. Since the signals have the receiver calibration corrections as well as the spin-phase rotation correction already performed, the X, Y, and Z signal components are already lined up with the RPI coordinate system, and the combined amplitude of the cross-products is representative of the real E-field strengths.

36 samples are used from each of the antennas to obtain 36 sets of power terms W and then calculate the averages:

$$Re[\langle W_{xy} \rangle] = \frac{1}{36} \sum_{i=1}^{36} Re[W_{xyi}]$$

$$Im[\langle W_{xy} \rangle] = \frac{1}{36} \sum_{i=1}^{36} Im[W_{xyi}]$$
(A-7)

These averages are not necessarily positive numbers, and in order to express the magnitude of the cross-power,  $CP_{XY}$ , we have to use  $\sqrt{\text{Re}^2 + \text{Im}^2}$ :

$$CP_{XY} = \sqrt{\text{Re}[\langle W_{XY} \rangle]^2 + \text{Im}[\langle W_{XY} \rangle]^2}$$
 (A-8)

And in dB,

$$CP_{XY\log} = 10\log_{10} \left( \operatorname{Re}[\langle W_{xy} \rangle]^2 + \operatorname{Im}[\langle W_{xy} \rangle]^2 \right)$$
(A-9)

#### A3. Calculating Cross Phases (XY, XZ and YZ)

Cross phase term,  $CPh_{XY}$ , is calculating as

$$CPh_{XY} = \arctan\left(\frac{\mathrm{Im}\left[\langle W_{xy} \rangle\right]}{\mathrm{Re}\left[\langle W_{xy} \rangle\right]}\right), \quad [\mathrm{range} \ -180\mathrm{deg} \ \mathrm{to} \ +179\mathrm{deg}] \tag{A-10}$$

and stored in [360/255] degree units as 8 bit integer. The terms  $CPh_{XZ}$  and  $CPh_{YZ}$  are calculated similarly.

### Appendix B. Coupler Band Center Frequency Table

Index	Frequency, kHz	Index	Frequency, kHz	Index	Frequency, kHz
0	3 000	46	45 600	92	193 500
1	9.500	47	47.150	93	195.000
2	9.900	48	48.700	94	195.750
3	10.200	49	51.600	95	198.000
4	10.450	50	54.500	96	200.000
5	10.800	51	56.025	97	205.000
6	11.150	52	57.550	98	220.000
7	11.600	53	59.425	99	233.000
8	11.950	54	61.300	100	259.000
9	12.500	55	63.325	101	308.000
10	13.100	56	65.350	102	320.000
11	13.500	57	68.300	103	380.000
12	13.750	58	72,700	104	440.000
13	14.300	59	74.550	105	496.000
14	14 750	60	76 400	106	535,000
15	15 350	61	78 850	107	575.000
16	15 800	62	81 200	108	605 000
17	16.500	63	84 900	109	630,000
18	17 350	64	86,000	110	653,000
19	17 900	65	89 800	111	685,000
20	18 300	66	97 400	112	760 000
21	18.950	67	100 500	113	870.000
22	19.600	68	102.500	114	904 000
23	20 400	69	105 000	115	973 000
24	21 000	70	108.000	116	1190 000
25	21.950	71	111.500	117	1220.000
26	23 000	72	114 000	118	1280.000
27	23.700	73	118.200	119	1320.000
28	24.150	74	134.500	120	1510.000
29	25.050	75	137.500	121	1600.000
30	25.900	76	139.750	122	2000.000
31	26.900	77	143.500	123	3000.000
32	27.700	78	146.000		
33	28.900	79	149.500		
34	30.600	80	151.500		
35	31.600	81	154.500		
36	32.300	82	172.000		
37	33.500	83	174.000		
38	34.500	84	175.500		
39	35.900	85	177.000		
40	37.000	86	180.000		
41	38.700	87	182.500		
42	40.400	88	185,000		
43	41.600	89	186,000		
44	42.550	90	190.500		
45	44 075	91	192,000		
10	11.070	/ <b>·</b>	172.000		

#### **Appendix C. Calibration Procedures**

#### C1. Phase calibration procedure

Phase calibration was done at SwRI labs by feeding a known generator signal into three receivers set at G=15, as shown on Figure C1-1.



Figure C1-1 Phase calibration setup with HP synthesizer

The output of each receiver was sampled twice, to capture I and Q quadrature components spaced 90° apart. The ratio of Z channel output to X and Y channels comprises the default calibration table.

#### C2. Onboard calibration procedure

Onboard calibration procedure is done by feeding identical calibration signals to the receivers on each frequency before the actual transmission is made, as shown in Figure C2-1. The calibration signal is applied directly to the couplers at the base of the X and Y antennas; however, the Z channel is calibrated without the wide-band pre-amplifiers whose gain is assumed equal to 12 dB (LoGain setting) and phase contributions are assumed constant for the mission period. The amplitude of the calibration signals is always the same and is selected optimally to obtain good receiver responses with any setting of their gain.

The receiver response to the calibration signals is used onboard to introduce corrections to the X and Y channel data that equalize their phase and gain characteristics with the Z channel. It is important to make +12 dB corrections to the X and Y data on the ground if HiGain setting was used for the Z preamplifier. With this correction introduced, RPI data can be directly used to derive the angles of arrival. An additional effort is required to convert the observed amplitudes to the physical units,  $[{}^{nV}/{}_{m}]$ , as discussed in Section 3.2.1.



Figure C2-1 Application of calibration signals to X(Y) and Z receiver channels

#### C3. Amplitude calibration procedure

Amplitude calibration was done at SwRI labs by feeding a known generator signal into receiver as shown on Figure C3-1.



Figure C3-1 Amplitude calibration setup with HP synthesizer

#### C3.1. Input voltage calculation

The generator input was originally expressed in [dBm into a 50 ohm load]. The following considerations are used to express the input voltage in [Vp]:

- dBm units are referenced to 1 mW of power on 50 ohm load
- Voltage corresponding to 1 mW on 50 ohm is:

$$V_{ref,rms} = \sqrt{1 \ mW \cdot 50 \ ohm} = \sqrt{0.05} \ [V]$$
$$V_{ref,p} = \sqrt{2} V_{ref,rms} = \sqrt{2} \ \sqrt{0.05} \ [V] = \sqrt{0.1} \ [V]$$

• For *D* dBm the generator output voltage is

$$V_{g\text{-out,p}} = V_{ref, p} * 10^{(D/20)} = \sqrt{0.1} * 10^{(D/20)} [V]$$

To account for the fact that the calibration setup (Figure C1-1) is different from the operational RPI setup where both dipole elements feed the receiver, 6 dB are subtracted from the test source power. Another 6 dB are subtracted to account for the losses in the 3 way splitter. Thus, the input voltage for this test is

$$V_{in,p} = \sqrt{0.1} * 10^{\frac{D-12}{20}} [V]$$

To obtain the value of receiver sensitivity in volts per digitizer unit,  $S_{du,p}(f)$ , from the amplitude calibration data, the following formula is used:

$$S_{du,p}(f) = \frac{V_{in,p}}{D_{out}(f)} \quad [V/unit],$$

where  $D_{out}(f)$  are the amplitudes [in digitizer units] and  $V_{in,p}$  is the peak voltage in [V].

#### C3.2. Amplitude calibration coefficients

Ratio of Z channel amplitudes to X and Y channel amplitudes gives the correction coefficients  $A'_{xc}$  and  $A'_{yc}$  for the re-calibration procedure described in Section 3.2.2.6. The coefficients are given in the Table C3-1.

#### C3.3. Physical Units table

Figure C3-1 shows graph of the Z channel zero-to-peak voltage per digitizer unit, in [nV/unit], which is used for conversion of the amplitudes to physical units in Section 3.2.2.8.



Figure C3-2 Z channel voltage per digitizer unit, [nV].

The gains of the X and Y channels are matched to the gain of the Z receiver during onboard calibration (see Section 3.1.2) so that, for the purpose of conversion to physical units, X and Y digitizer unit values are not used. The zero-to-peak voltage [in nV] per digitizer units for Z channel are given in Table C3-1. Section 3.2.2.3 explains how to use these coefficients to derive the Physical Units table for all channels and all settings of the base gain.

Frequency	Correction	Correction	Voltage ner
[kHz]	conficient A'	$conficient \Lambda'$	digitizer unit
[MI2]	coefficient $A_{xc}$	coefficient $A_{yc}$	[nVn]
7	36.786	34.606	1.971
8	32.217	27.144	1.691
9	21.343	17.426	1.712
10	20.693	36.123	1.549
11	26.149	44.490	1.168
12	20.990	24.373	1.777
13	9.402	13.094	4.328
14	15.622	18.961	3.123
15	13.994	12.361	3.653
16	11.783	8.955	2.784
17	33.190	17.836	1.448
18	22.553	42.523	1.343
19	17.918	15.358	1.933
20	16.976	31.871	1.961
21	6.800	21.410	3.704
22	17.677	16.946	2.885
23	17.989	19.127	1.632
24	13.724	37.506	1.466
25	19.310	49.934	1.404
26	13.823	30.128	2.058
27	23.085	52.569	1.368
28	14.056	60.605	1.991
29	18.772	57.071	1.976
30	45.052	81.761	1.694
31	17.635	103.667	1.546
32	31.611	50.388	1.781
33	34.732	62.367	1.564
34	20.254	36.133	2.218
35	19.757	21.180	2.212
36	18.400	19.822	2.398
37	26.678	19.183	2.896
38	7.088	19.022	4.213
39	6.840	10.953	8.295
40	15.872	16.209	4.524
41	9.065	18.823	4.449
42	27.071	17.596	3.110
43	18.585	11.252	3.721
44	24.816	12.849	2.699
45	28.564	18.269	1.937
46	14.459	18.870	2.619
47	20.235	11.917	3.418
48	9.354	9.119	5.137
49	23.868	32.905	3.942
50	21.188	19.133	3.923
51	12.420	36.054	2.520
52	29.292	19.059	1.887
53	8.975	8.446	3.774
54	22.224	28.051	1.856

 Table C3-1
 X/Y Amplitude Corrections and Physical Units table.

55	17.610	11.222	2.577
56	11.562	6.374	5.239
57	29.261	22.636	2.672
58	21.563	22.680	3.942
59	25.213	59.568	1.785
60	45.268	35.479	1.742
61	15.244	45.731	2.230
62	24.538	48.890	1.739
63	13.188	30.593	3.304
64	35.684	33.205	2.042
65	9.342	11.769	4.424
66	11.581	16.730	3,539
67	17.590	36.974	2.428
68	15.297	22.594	2.854
69	11.875	17.102	3.738
70	25.838	25.037	3.704
71	10.403	12.801	5.942
72	22.157	12.810	4.977
73	30.716	27.777	3.865
74	14 420	18 720	4 281
75	8 577	17 863	4 946
76	13 445	30.042	2.465
70	22 596	41 567	2.103
78	49 523	29.462	2.037
79	14 400	11 364	4 022
80	16 653	10.077	4.022
81	34 891	39.038	2 356
82	18 386	9 488	4 740
83	25 315	39 431	2 342
84	15 746	23 405	3 250
85	18 788	15 823	5.230
86	40 319	18.063	4 169
87	43 113	19 452	3 884
88	39 570	34 594	3 884
89	19.636	33 790	3 224
90	25 350	14 358	4 236
91	3 019	29.121	3 670
92	25 115	33 200	2 315
93	23.115	37 368	2.515
94	8 724	10 383	12 639
95	63 335	93 084	2 435
96	29 208	34 685	6 221
97	19 501	26 168	12 251
98	32 935	33 748	8 200
99	34 474	15 712	12 630
100	27.3/4	24 015	<u>8 125</u>
101	13 21/	0 863	16 251
102	22 010	16 259	7 884
102	12 607	10.330	11 710
103	17 867	10 526	\$ 200
105	16.077	19.520	0.209
105	16.077	10.700	7.500
100	10.228	13.900	7.110
107	12.299	14.229	1.131

108	15.828	14.383	6.474
109	25.354	17.031	5.729
110	17.699	17.278	7.731
111	16.565	14.466	10.341
112	12.685	10.554	8.209
113	14.753	10.991	10.209
114	10.074	14.180	10.080
115	11.926	7,943	10.908
116	21.001	12.682	6.806
117	20.359	10.752	8.382
118	6 305	9 523	16 251
119	16 798	26 434	6 581
120	23 307	16 712	5 204
120	19 995	12,782	6 270
121	23 611	15 531	6 422
122	18.062	16 589	9 594
125	17 703	21 532	5 855
125	9 714	8 704	7 884
125	14 386	22 749	5 942
120	25 434	18 045	4 915
127	17 767	15.616	9 1 5 3
120	28.002	24 155	5 104
130	8 663	9 238	10 080
131	6 312	6.178	13 970
132	6 728	9 394	15.024
133	6 933	7 804	14 746
134	7 136	6 298	13 496
135	17 465	19.682	9 049
136	13 504	11 332	6 924
137	15.085	9 1 2 6	8 750
138	6.499	11.481	14.478
139	11.321	9.636	8.562
140	12.798	20.977	8.043
141	13.108	18.182	7.963
142	6.574	9.818	14.746
143	12.421	18.075	8.562
144	9.433	8.350	9.954
145	25.469	11.797	7.373
146	13.652	10.816	7.305
147	21.252	16.727	8.655
148	32.431	13.486	5.492
149	6.883	6.569	11.540
150	16.721	12.934	5.273
151	6.155	6.172	10.477
152	17.773	13.965	7.174
153	10.568	9.557	6.806
154	13.076	10.216	9.153
155	19.648	21.449	5.812
156	14.772	9.907	7.731
157	26.792	12.853	5.898
158	12.733	21.769	6.173
159	13.038	8.004	8.295
160	15.014	23.208	6.320

161	21.317	20.401	6.748
162	13.308	21.225	6.691
163	12.567	10.689	12.065
164	7.428	5.338	11.710
165	15.918	13.064	5.008
166	8.476	8.772	9.954
167	14.371	12.777	5.647
168	8 184	7 510	8 209
169	10 648	10 248	6 865
170	27 222	19 983	5 104
171	6 976	8 006	10.617
172	6 718	12 690	10.341
172	14 378	12.000	5 309
173	10.088	9 784	8 655
174	14 863	18 / 83	7 884
175	12 483	18 225	7.88 <del>4</del> 8.043
170	10.726	10.233	7 807
178	6 011	14.01/ 6 976	12 054
170	20.011	0.870	6 749
1/9	12 001	9.007	7 110
180	12.001	18.420	6 806
182	2 508	10.420	6.527
182	20 221	24 183	6.327
183	20.221	24.103	8 8 4 8
104	7 422	5.022	0.046
185	12 141	7.022	0.504
180	13.141	7.930	9.394
107	0.552	10.429	13.490
180	6 3 5 1	11 512	8 205
109	8 857	11.312	12.065
190	11 366	6.615	12.003
191	6 169	10.070	12 720
192	0.108	10.970	10,200
195	11 209	7.620	10.209
194	11.308	11 272	6 749
193	13.911	11.2/3	0.748
190	10.300	12.281	/.110
197	(.//4	14.434	9.480
198	6.820	11.903	11./10
199	0.012	8.034	12.639
200	39.1/8	53.870	1.602
201	13.195	12./2/	11.3/3
202	6.252	/.380	12.251
203	5.333	/.015	13.729
204	11.540	14.550	8.382
205	6.451	11.460	13.054
206	19.874	12.594	6.527
207	10.833	9.087	11.540
208	11.365	8.220	16.251
209	11.2/3	8.372	11.215
210	22.545	10.323	7.963
211	14.340	11.332	6.924
212	6.980	7.098	11.885
213	14.365	13.972	6.748

214	18.743	14.399	5.688
215	6.263	6.066	12.251
216	11.234	6.054	13.729
217	17.927	11.291	6.370
218	16.620	12.561	6.924
219	16.209	12.157	9.049
220	10.645	10.417	7.110
221	22.216	13.233	7.373
222	9.361	9.140	8.295
223	11.781	11.733	7.807
224	7.809	8.239	11.540
225	13.115	7.217	9.480
226	6.507	10.706	11.710
227	4.035	14.873	8.382
228	14.663	16.396	8.295
229	10.957	9.745	7.174
230	13.139	18.744	5.492
231	11.834	11.529	5.898
232	12.752	13.951	5.309
233	8.394	8.014	8.750
234	12.885	27.991	5.417
235	6.729	8.967	10.341
236	10.190	10.953	8.295
237	26 762	16 533	6.032
238	14 062	14 998	6 422
239	13 386	9 494	8 382
240	11 912	20 756	6 474
241	13 413	18 000	8 043
242	9 755	9.809	12 639
243	6 640	11 110	19 422
244	17 871	11 150	8 750
245	19 177	17 905	6 924
246	21 714	11 418	8 471
247	4 921	5 308	18 959
248	8 019	8 019	11 375
249	10.867	12 097	8 750
250	9 960	12.037	9 368
251	7 454	6 610	13 970
252	12.782	11 337	7 584
253	13 741	25 793	7 373
253	10 781	12 100	10.080
255	6 464	6 250	13 970
255	13 647	22.912	7 963
257	12 972	8 741	13 729
258	12.972	12 005	10.617
250	6 005	3 627	24 808
200	0.003	5.052 6.415	15 069
280	1/ 2/4	7 201	13.000
200	14.240	2.371 8.204	10.752
300	10.047	0.204	10.732
310	21.010	12 570	12.700
320	12 645	5 202	10.510
320	12.043	J.303 12 420	13.790
330	14.390	12.438	13.327

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340	8.071	5.989	16.220
350	11.127	6.334	15.081
360	14.185	7.170	10.393
370	14.406	8.015	12.407
380	12.546	7.335	10.632
390	5.538	3.951	26.371
400	4.226	5.123	24.318
410	11.859	7.906	10.096
420	9.283	6.814	14.680
430	5.134	3.738	34.714
440	11.886	10.814	16.694
450	5.419	3.888	23.333
460	9.923	6.501	14.926
470	11.018	6.068	21.529
480	12.622	4.512	20.657
490	4.186	4.568	28.879
500	12.762	9.662	17.978
510	6.934	5.365	17.008
520	8.096	6.064	20.086
530	15.782	9.848	14.645
540	8.360	6.349	15.278
550	9,609	13.985	14,496
560	15.908	15.854	10.749
570	16 476	14 520	9 011
580	12 335	10 969	17 339
590	16 389	10.903	14 639
600	8 679	3 668	25.418
610	10 504	11 823	15 054
620	7 686	5 708	15 401
630	11 699	9 945	13 936
640	9.394	7.385	12,102
650	8.641	7.266	13.649
660	5.147	6.420	24.133
670	10.500	7.525	19.637
680	5.899	5.443	16.740
690	11.646	7.234	17.254
700	7.315	4.102	24,787
710	20.112	5.407	23.588
720	7.770	2.583	68.821
730	4.549	6.102	49.537
740	3.487	4.105	74.168
750	5.608	3.872	30.909
760	3.231	4.666	24.081
770	7.055	4.718	23.472
780	9.058	5.052	36.278
790	8.240	7.505	21.753
800	9 705	4 202	29 687
810	10 111	10 224	18 353
820	10 725	11.547	15 085
830	13 357	12 610	15 337
840	7 370	6 775	26 837
850	8 788	4 528	22.722
860	6.852	8.163	22.084
		0.000	==

870	10.045	8.069	14.374
880	7.056	7.056	23.909
890	9.935	7.108	15.566
900	8.285	4.498	24.177
910	7.471	5.942	24.695
920	10.427	7.085	15.555
930	83.906	14.703	14.461
940	14.034	8.285	21.931
950	20.491	9.025	18.007
960	17.326	10.957	22.342
970	13.099	10.088	14.597
980	9.927	7.120	22.223
990	15.436	5.756	23.764
1000	11.128	5.875	25.312
1010	8.934	5.790	31.958
1020	14.139	5.598	28.424
1030	7.726	3.159	40.426
1040	13.438	4.366	34.025
1050	12.553	3.194	34.428
1060	20.506	5.870	20.650
1070	5.595	3.223	34.696
1080	6.305	3.470	32.598
1090	7.968	6.390	32.455
1100	9.792	9.514	11.071
1110	10.004	5.325	15.847
1120	17.597	8.054	16.677
1130	16.327	8.679	12.671
1140	23.271	8.588	10.428
1150	10.912	5.540	14.980
1160	8.490	5.469	20.250
1170	10.175	4.211	19.562
1180	9.854	6.773	16.048
1190	15.427	10.767	10.995
1200	55.145	10.278	12.856
1210	11.495	4.431	21.696
1220	13.186	4.636	20.536
1230	23.027	12.315	11.417
1240	7.945	4.747	19.853
1250	19.740	10.518	14.867
1260	12.242	6.846	22.508
1270	16.123	10.157	15.716
1280	12.524	6.904	12.918
1290	14.368	5.578	17.021
1300	10.559	3.583	25.982
1310	8.321	11.487	13.421
1320	12.836	7.841	20.740
1330	15.849	10.231	13.727
1340	14.013	11.172	13.014
1350	18.286	9.131	12.547
1360	9.794	4.942	20.195
1370	11.634	5.776	23.892
1380	9.975	3.726	28.364
1390	13.429	8.453	17.730

1400	8.423	7.334	24.723
1410	11.832	6.333	19.392
1420	5.719	5.469	33.033
1430	15.598	8.610	17.820
1440	7.639	4.463	25.811
1450	10.007	5.672	20.948
1460	10.216	6.066	20.657
1470	7.441	5.346	29.859
1480	38.719	12.659	12.731
1490	15.110	13.443	11.441
1500	15.453	7.204	12.881
1510	9.255	5.450	17.259
1520	22.341	7.366	13.259
1530	17.859	10.047	11.145
1540	11 766	12 660	11.056
1550	15 502	10 655	11.832
1560	23 361	11 015	14 840
1570	12 000	8 829	19 120
1580	16 733	9 917	12.782
1590	24 856	8 650	14 758
1600	20 929	10 446	10.616
1610	24 382	10 715	13 913
1620	13 658	7 647	16 677
1630	27.832	7 793	15 013
1640	15 107	5 058	24 282
1650	15 240	7 583	16 173
1660	9.587	4,911	25.217
1670	16.256	5.645	22.179
1680	10.434	5.404	23.621
1690	20.190	11.801	15.783
1700	16.985	14.257	14.288
1710	18.762	6.351	22.877
1720	16.314	9.970	20.682
1730	14.882	10.098	17.165
1740	9.748	7.070	19.978
1750	18.362	7.462	19.978
1760	16.568	8.525	16.275
1770	25.735	11.713	15.716
1780	17.243	10.324	17.425
1790	25.735	9.560	14.950
1800	21.279	6.938	19.900
1810	18.866	8.871	15.555
1820	30.486	10.303	14.176
1830	10.831	5.824	23.680
1840	24.130	11.531	17.317
1850	32.220	12.879	14.294
1860	14.236	11.589	19.104
1870	20.762	8.586	16.339
1880	21.271	9.771	16.665
1890	20.983	13.964	15.581
1900	21.163	7.062	20.562
1910	33.354	13.330	15.764
1920	22.529	11.792	16.974

1930         24.196         6.926         22.676           1940         15.450         8.283         21.161           1950         21.298         9.241         20.863           1960         15.847         7.984         22.120           1970         16.708         9.300         23.456           1980         18.155         10.785         19.308           1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         24.4719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.231           2080         19.094         8.239         22.327           2090         27.660         13.077         16.41           210         23.006         13.403         19.314				
1940         15.450         8.283         21.161           1950         21.298         9.241         20.863           1960         15.847         7.984         22.120           1970         16.708         9.300         23.456           1980         18.155         10.785         19.308           1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.338         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.321           2080         19.904         8.239         22.327           2090         27.660         13.077         16.411           2100         23.006         13.403         19.314           2130         26.375         11.497         17.590	1930	24.196	6.926	22.676
1950         21.298         9.241         20.863           1960         15.847         7.984         22.120           1970         16.708         9.300         23.456           1980         18.155         10.785         19.308           1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.134           2070         31.536         10.387         22.231           2080         19.094         8.239         23.327           2100         24.789         9.566         18.995           2110         20.502         10.019         21.982           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590	1940	15.450	8.283	21.161
1960         15.847         7.984         22.120           1970         16.708         9.300         23.456           1980         18.155         10.785         19.308           1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.31           2080         19.094         8.239         22.327           2090         27.660         13.077         16.41           2100         23.906         13.403         19.314           2130         26.375         11.497         17.590           2140         21.260         11.135         16.307           2150         25.100         10.565         16.871	1950	21.298	9.241	20.863
1970         16.708         9.300         23.456           1980         18.155         10.785         19.308           1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.338         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.237           2080         19.094         8.239         22.327           2090         27.660         13.077         16.411           2100         23.006         13.403         19.314           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590           2140         21.260         11.135         16.307           2150         25.100         10.565         16.871	1960	15.847	7.984	22.120
1980         18.155         10.785         19.308           1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.231           2080         19.094         8.239         22.327           2090         27.660         13.077         16.411           2100         24.789         9.566         18.995           2110         20.502         10.019         21.982           2130         26.375         11.497         17.590           2140         21.260         11.135         16.307           2150         25.100         10.565         16.871           2160         28.702         14.285         15.444	1970	16.708	9.300	23.456
1990         27.439         10.340         15.537           2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.231           2080         19.094         8.239         22.327           2090         27.660         13.077         16.411           2100         24.789         9.566         18.995           2110         20.502         10.019         21.982           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590           2140         21.600         10.135         16.307           2160         28.372         14.285         15.444           2170         28.563         18.720         14.251	1980	18.155	10.785	19.308
2000         20.660         10.024         22.622           2010         20.151         10.621         21.446           2020         19.490         11.485         21.439           2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.327           2090         27.660         13.077         16.411           2100         23.006         13.403         19.314           2110         20.502         10.019         21.982           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590           2140         21.260         11.135         16.307           2150         25.100         10.565         16.871           2160         28.372         14.285         15.444           2170         28.702         12.349         14.853           2180         25.367         15.240         16.694	1990	27.439	10.340	15.537
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2000	20.660	10.024	22.622
2020 $19.490$ $11.485$ $21.439$ $2030$ $24.855$ $12.918$ $17.507$ $2040$ $44.388$ $15.294$ $16.339$ $2050$ $44.719$ $11.430$ $15.010$ $2060$ $23.496$ $10.559$ $22.194$ $2070$ $31.536$ $10.387$ $22.231$ $2080$ $19.094$ $8.239$ $22.327$ $2090$ $27.660$ $13.077$ $16.411$ $2100$ $24.789$ $9.566$ $18.995$ $2110$ $20.502$ $10.019$ $21.982$ $2120$ $23.006$ $13.403$ $19.314$ $2130$ $26.375$ $11.497$ $17.590$ $2140$ $21.260$ $11.135$ $16.307$ $2150$ $25.100$ $10.565$ $16.871$ $2160$ $28.372$ $14.285$ $15.444$ $2170$ $28.702$ $12.349$ $14.853$ $2180$ $25.367$ $15.240$ $16.694$ $2190$ $28.563$ $18.720$ $14.251$ $2200$ $17.094$ $10.119$ $25.633$ $2210$ $27.706$ $10.307$ $18.218$ $2230$ $28.496$ $13.667$ $15.376$ $2240$ $35.033$ $15.256$ $13.341$ $2250$ $19.134$ $9.728$ $21.838$ $2260$ $23.721$ $16.005$ $17.272$ $2270$ $24.485$ $11.318$ $17.303$ $2280$ $23.678$ $10.983$ $17.303$ $2290$ $22.605$ $11.817$ $18.364$ $2300$ <	2010	20.151	10.621	21.446
2030         24.855         12.918         17.507           2040         44.388         15.294         16.339           2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.231           2080         19.094         8.239         22.327           2090         27.660         13.077         16.411           2100         23.006         13.403         19.314           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590           2140         21.260         11.135         16.307           2150         25.100         10.565         16.871           2160         28.372         14.285         15.444           2170         28.702         12.349         14.853           2180         25.367         15.240         16.694           2190         28.563         18.720         14.251           2200         17.094         10.119         25.633           2210         27.706         10.307         18.218	2020	19.490	11.485	21.439
2040 $44.388$ $15.294$ $16.339$ $2050$ $44.719$ $11.430$ $15.010$ $2060$ $23.496$ $10.559$ $22.194$ $2070$ $31.536$ $10.387$ $22.231$ $2080$ $19.094$ $8.239$ $22.327$ $2090$ $27.660$ $13.077$ $16.411$ $2100$ $24.789$ $9.566$ $18.995$ $2110$ $20.502$ $10.019$ $21.982$ $2120$ $23.006$ $13.403$ $19.314$ $2130$ $26.375$ $11.497$ $17.590$ $2140$ $21.260$ $11.135$ $16.307$ $2150$ $25.100$ $10.565$ $16.871$ $2160$ $28.372$ $14.285$ $15.444$ $2170$ $28.702$ $12.349$ $14.853$ $2180$ $25.367$ $15.240$ $16.694$ $2190$ $28.563$ $18.720$ $14.251$ $2200$ $17.094$ $10.119$ $25.633$ $2210$ $27.706$ $10.307$ $18.218$ $2230$ $28.496$ $13.667$ $15.376$ $2240$ $23.503$ $15.256$ $13.341$ $2250$ $19.134$ $9.728$ $21.838$ $2260$ $23.721$ $16.005$ $17.272$ $2270$ $24.485$ $11.318$ $17.303$ $2280$ $23.678$ $10.983$ $17.303$ $2290$ $22.605$ $11.817$ $18.364$ $2300$ $30.133$ $12.917$ $15.664$ $2310$ $22.827$ $14.063$ $19.465$ $2340$ <	2030	24.855	12.918	17.507
2050         44.719         11.430         15.010           2060         23.496         10.559         22.194           2070         31.536         10.387         22.231           2080         19.094         8.239         22.327           2090         27.660         13.077         16.411           2100         24.789         9.566         18.995           2110         20.502         10.019         21.982           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590           2140         21.200         10.019         21.982           2150         25.100         10.555         16.871           2160         28.372         14.285         15.444           2170         28.702         12.349         14.853           2180         25.367         15.240         16.694           2190         28.563         18.720         14.251           2200         17.094         10.119         25.633           2210         27.706         10.307         18.218           2230         28.496         13.667         15.376	2040	44.388	15.294	16.339
2060         23.496         10.559         22.194           2070         31.536         10.387         22.231           2080         19.094         8.239         22.327           2090         27.660         13.077         16.411           2100         24.789         9.566         18.995           2110         20.502         10.019         21.982           2120         23.006         13.403         19.314           2130         26.375         11.497         17.590           2140         21.260         11.135         16.307           2150         25.100         10.565         16.871           2160         28.372         14.285         15.444           2170         28.702         12.349         14.853           2180         25.367         15.240         16.694           2190         28.563         18.720         14.251           2200         17.06         10.307         18.218           2230         28.496         13.667         15.376           2240         35.033         15.256         13.341           2250         19.134         9.728         21.838	2050	44.719	11.430	15.010
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2060	23.496	10.559	22.194
2080 $19.094$ $8.239$ $22.327$ $2090$ $27.660$ $13.077$ $16.411$ $2100$ $24.789$ $9.566$ $18.995$ $2110$ $20.502$ $10.019$ $21.982$ $2120$ $23.006$ $13.403$ $19.314$ $2130$ $26.375$ $11.497$ $17.590$ $2140$ $21.260$ $11.135$ $16.307$ $2150$ $25.100$ $10.565$ $16.871$ $2160$ $28.372$ $14.285$ $15.444$ $2170$ $28.702$ $12.349$ $14.853$ $2180$ $25.367$ $15.240$ $16.694$ $2190$ $28.563$ $18.720$ $14.251$ $2200$ $17.094$ $10.119$ $25.633$ $2210$ $27.706$ $10.307$ $18.218$ $2230$ $27.706$ $10.307$ $18.218$ $2230$ $28.496$ $13.667$ $15.376$ $2240$ $35.033$ $15.256$ $13.341$ $2250$ $19.134$ $9.728$ $21.838$ $2260$ $23.721$ $16.005$ $17.272$ $2270$ $24.485$ $11.318$ $17.303$ $2280$ $23.678$ $10.983$ $17.303$ $2290$ $22.605$ $11.817$ $18.364$ $2300$ $23.678$ $10.983$ $17.303$ $2290$ $22.605$ $11.817$ $18.364$ $2300$ $23.575$ $14.4637$ $15.584$ $2340$ $26.014$ $14.991$ $17.834$ $2350$ $23.838$ $19.029$ $14.635$ $2340$	2070	31.536	10.387	22.231
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2080	19.094	8.239	22.327
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2090	27.660	13.077	16.411
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2100	24.789	9.566	18.995
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2110	20.502	10.019	21.982
2130 $26.375$ $11.497$ $17.590$ $2140$ $21.260$ $11.135$ $16.307$ $2150$ $25.100$ $10.565$ $16.871$ $2160$ $28.372$ $14.285$ $15.444$ $2170$ $28.702$ $12.349$ $14.853$ $2180$ $25.367$ $15.240$ $16.694$ $2190$ $28.563$ $18.720$ $14.251$ $2200$ $17.094$ $10.119$ $25.633$ $2210$ $29.791$ $16.614$ $14.607$ $2220$ $27.706$ $10.307$ $18.218$ $2230$ $28.496$ $13.667$ $15.376$ $2240$ $35.033$ $15.256$ $13.341$ $2250$ $19.134$ $9.728$ $21.838$ $2260$ $23.721$ $16.005$ $17.272$ $2270$ $24.485$ $11.318$ $17.303$ $2280$ $23.678$ $10.983$ $17.303$ $2290$ $22.605$ $11.817$ $18.364$ $2310$ $27.029$ $11.162$ $17.420$ $2320$ $25.156$ $14.553$ $17.916$ $2330$ $22.827$ $14.063$ $19.465$ $2340$ $26.014$ $14.991$ $17.834$ $2350$ $23.373$ $16.356$ $17.416$ $2340$ $26.372$ $16.091$ $16.615$ $2340$ $23.373$ $16.356$ $17.416$ $2400$ $23.373$ $16.356$ $17.416$ $2400$ $23.373$ $16.356$ $17.416$ $2410$ $28.522$ $16.096$ $17.697$ $2440$	2120	23.006	13.403	19.314
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2130	26.375	11.497	17.590
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2140	21.260	11.135	16.307
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2150	25.100	10.565	16.871
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2160	28.372	14.285	15.444
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2170	28.702	12.349	14.853
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2180	25.367	15.240	16.694
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2190	28.563	18.720	14.251
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2200	17.094	10.119	25.633
2220 $27.706$ $10.307$ $18.218$ $2230$ $28.496$ $13.667$ $15.376$ $2240$ $35.033$ $15.256$ $13.341$ $2250$ $19.134$ $9.728$ $21.838$ $2260$ $23.721$ $16.005$ $17.272$ $2270$ $24.485$ $11.318$ $17.530$ $2280$ $23.678$ $10.983$ $17.303$ $2290$ $22.605$ $11.817$ $18.364$ $2300$ $30.133$ $12.917$ $15.064$ $2310$ $27.029$ $11.162$ $17.420$ $2320$ $25.156$ $14.553$ $17.916$ $2330$ $22.827$ $14.063$ $19.465$ $2340$ $26.014$ $14.991$ $17.834$ $2350$ $23.838$ $19.029$ $14.543$ $2360$ $28.934$ $14.879$ $14.635$ $2370$ $26.372$ $16.091$ $16.615$ $2380$ $30.514$ $18.837$ $13.971$ $2390$ $24.486$ $16.397$ $17.294$ $2400$ $23.373$ $16.356$ $17.416$ $2410$ $28.109$ $14.547$ $15.588$ $2420$ $33.236$ $19.531$ $13.093$ $2430$ $28.522$ $16.096$ $17.697$ $2440$ $34.712$ $16.634$ $12.623$ $2450$ $30.599$ $18.734$ $15.274$	2210	29,791	16.614	14.607
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2220	27.706	10.307	18.218
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2230	28,496	13.667	15.376
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2240	35.033	15.256	13.341
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2250	19.134	9.728	21.838
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2260	23.721	16.005	17.272
$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	2270	24.485	11.318	17.530
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2280	23.678	10.983	17.303
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2290	22.605	11.817	18.364
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2300	30,133	12.917	15.064
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2310	27.029	11.162	17.420
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2320	25.156	14.553	17.916
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	2330	22.827	14.063	19.465
2350         23.838         19.029         14.543           2360         28.934         14.879         14.635           2370         26.372         16.091         16.615           2380         30.514         18.837         13.971           2390         24.486         16.397         17.294           2400         23.373         16.356         17.416           2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2340	26.014	14.991	17.834
2360         28.934         14.879         14.635           2370         26.372         16.091         16.615           2380         30.514         18.837         13.971           2390         24.486         16.397         17.294           2400         23.373         16.356         17.416           2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2350	23.838	19.029	14.543
2370         26.372         16.091         16.615           2380         30.514         18.837         13.971           2390         24.486         16.397         17.294           2400         23.373         16.356         17.416           2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2360	28.934	14.879	14.635
2380         30.514         18.837         13.971           2390         24.486         16.397         17.294           2400         23.373         16.356         17.416           2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2370	26.372	16.091	16.615
2390         24.486         16.397         17.294           2400         23.373         16.356         17.416           2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2380	30.514	18.837	13.971
2400         23.373         16.356         17.416           2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2390	24.486	16.397	17.294
2410         28.109         14.547         15.588           2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2400	23 373	16 356	17 416
2420         33.236         19.531         13.093           2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2410	28.109	14 547	15 588
2430         28.522         16.096         17.697           2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2420	33 236	19.531	13 093
2440         34.712         16.634         12.623           2450         30.599         18.734         15.274	2430	28 522	16 096	17 697
2450 30.599 18.734 15.274	2440	34 712	16.634	12 623
	2450	30.599	18.734	15.274

2460	25.800	17.529	16.196
2470	29.656	18.546	13.815
2480	32.854	16.769	13.065
2490	27.569	17.346	15.156
2500	31.357	17.022	13.238
2510	27.330	17.652	15.922
2520	27.369	18.414	15.790
2530	28.882	19.299	14.963
2540	26.054	13.548	16.935
2550	27.661	17.956	16.064
2560	32.971	20.663	12.844
2570	26.677	14.958	16.656
2580	25.225	13.706	17.740
2590	27.060	18.437	15.862
2600	26.859	18.006	15.661
2610	33.792	18.068	14.039
2620	26.937	14.877	17.223
2630	28.366	14.507	15.888
2640	28.266	13.289	17.716
2650	23.302	17.373	19.765
2660	27.276	15.803	18.506
2670	30.123	16.711	18.374
2680	25.276	16.762	19.812
2690	23.274	14.628	19.364
2700	33.492	24.340	15.316
2710	31.739	24.597	15.292
2720	30.819	17.004	15.994
2730	23.347	15.845	20.473
2740	31.319	22.923	15.617
2750	31.017	13.442	20.342
2760	31.151	19.499	16.467
2770	24.898	17.809	19.494
2780	28.714	17.870	17.721
2790	33.242	22.629	15.687
2800	33.293	19.662	15.926